

# **Bulk Properties and Collective Dynamics**

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Many thanks to the conference organizers

## 1) Introduction

- Hydrodynamic approach
- Collectivity, local thermalization

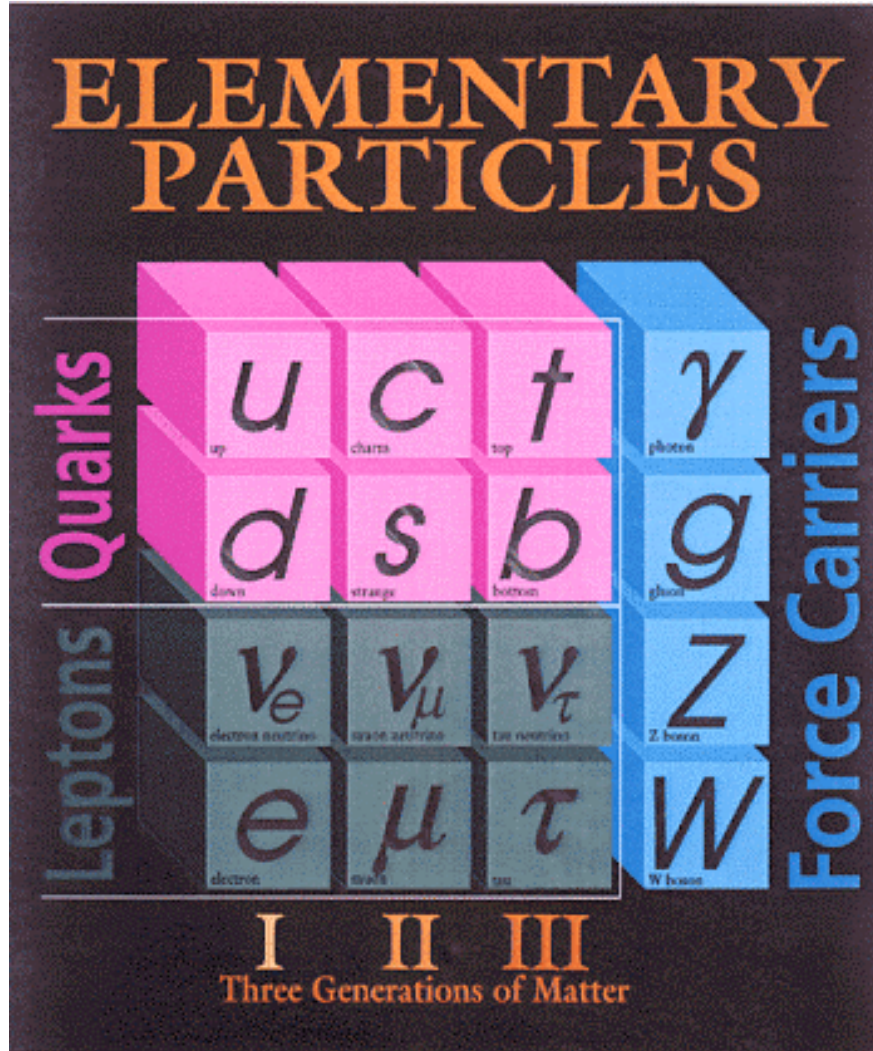
## 2) Recent experimental data

- Transverse momentum distributions
- Partonic collectivity at RHIC

## 3) Summary and outlook



# Quantum Chromodynamics

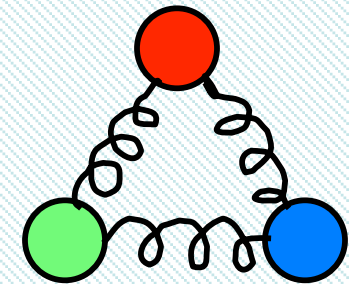


- 1) Quantum Chromodynamics (QCD) is the established theory of strongly interacting matter.
- 2) Gluons hold quarks together to form hadrons:

meson



baryon



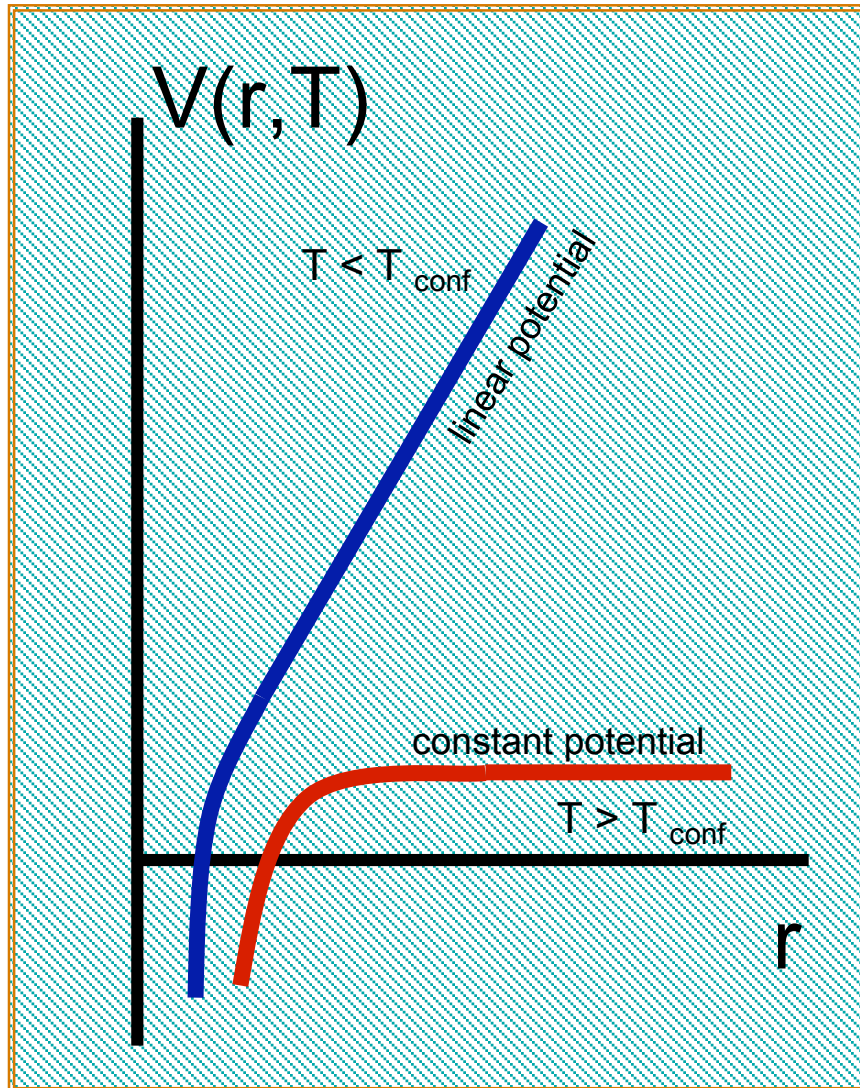
- 3) Gluons and quarks, or partons, typically exist in a color singlet state: confinement.

“In high-energy physics we have concentrated on experiments in which we distribute a higher and higher amount of energy into a region with smaller and smaller dimensions.

In order to study the question of ‘**vacuum**’, we must turn to a different direction; we should investigate some ‘**bulk**’ **phenomena** by distributing high energy over a relatively large volume.”

Prof. T.D. Lee, Rev. Mod. Phys. 47, 267(1975).

# Confinement Potential



The potential between quarks is a function of distance. It also depends on the temperature.

1) At low temperature, the potential increases linearly with the distance between quarks

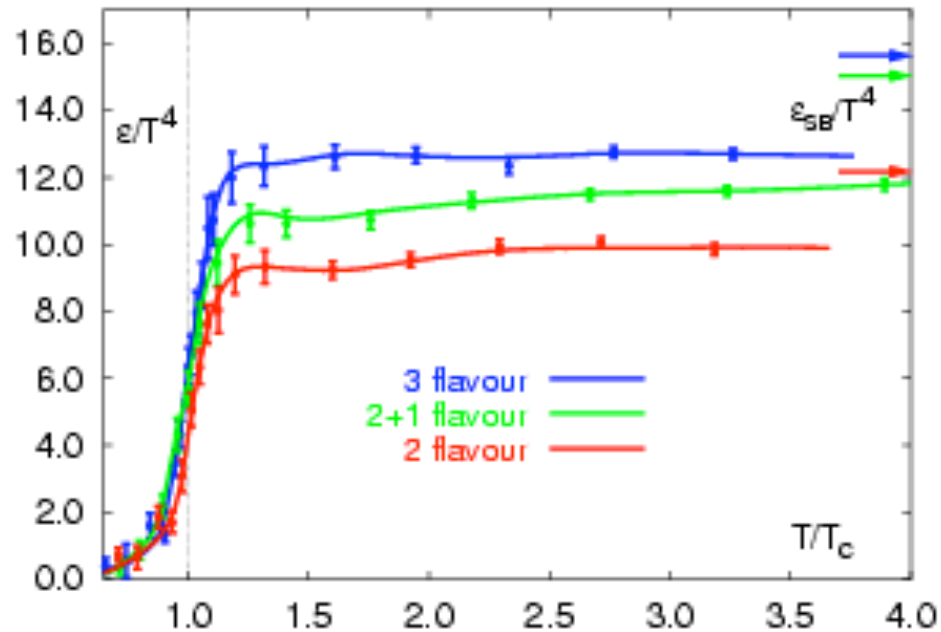
⇒ quarks are confined;

2) At high temperature, the confinement potential is 'melted'

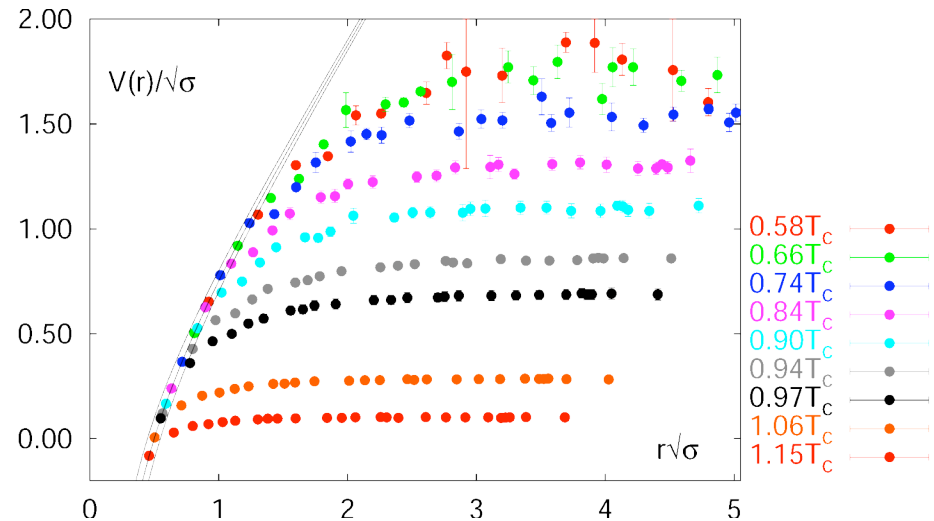
⇒ quarks are 'free'.

Note: It is not clear at all if there is a critical 'temperature' in high energy collisions

## Energy density



## Heavy quark potential



- Left: Large increase in energy density at  $T_c \sim 170$  MeV.  
Not reach the non-interacting S.B. limit.
- Right: Heavy quark potentials are melted at high temperature.

*F. Karsch et al. Nucl. Phys. **B524**, 123(02). Z. Fodor et al, **JHEP** 0203:014(02).  
C.R. Allton et al, Nucl. Rev. **D66**, 074507(02). F. Karsch, Nucl. Phys. **A698**, 199c(02).*

# What Is the Problem ?

## - The confinement:

Quarks are the basic building blocks of matter.

No free quarks are seen, confined within hadron:

$$\Delta v_0 \sim 1 \text{ fm}^3, \quad \rho_0 \sim 0.16 \text{ fm}^{-3}, \quad \varepsilon_0 \sim 0.15 \text{ GeV/fm}^3$$

## - Heavy ion collisions: Large, hot, and dense system

$$\begin{aligned} \Delta v &\sim 1000 \text{ fm}^3 = 1000 v_0 \\ \rho &\gg 3 \text{ fm}^{-3} \sim 20 \rho_0 \\ \varepsilon &\gg 3 \text{ GeV/fm}^3 \sim 20 \varepsilon_0 \end{aligned} \quad \Rightarrow \text{QGP(?)}$$

Quarks and gluons are ‘freely’ moving in a large volume

New form of ***matter with partonic degrees of freedom***

## - Connection with other fields

cosmology, origin of the universe, evolution of the universe

quantum statistics with partons

# Statistical QCD and dof

$$\varepsilon_{QED} = \frac{\pi^2}{30} \left[ 2 + \frac{7}{8} 2 \times 2 \right] T^4$$

photon spin

electron spin

$$\varepsilon_{QCD} = \frac{\pi^2}{30} \left[ 2 \times 8 + \frac{7}{8} 2 \times 2 \times 3 \times 3 \right] T^4$$

gluon spin, color

quark spin, color, flavor

***Energy density reflects on what the matter is made of !***

# Hadron $\Leftrightarrow$ Quark-gluon Gas

## 1) Facts:

- hadron radius  $r_h \sim 1$  fm
- $T \geq T_c \sim 1/r_h = 0.2$  GeV

## 2) Hadron to parton transition $T \geq T_c$ GC partition function becomes divergent

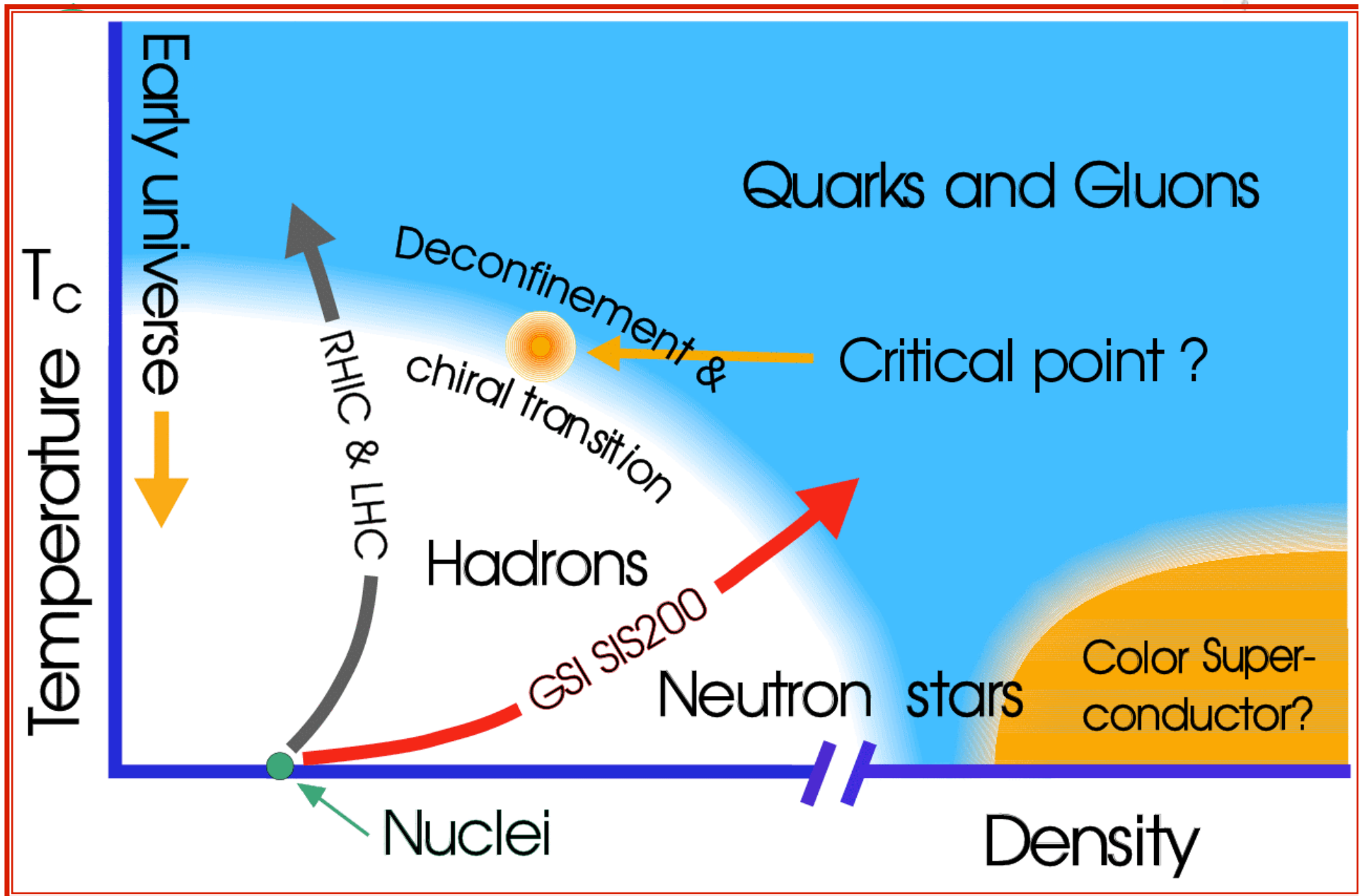
*I. Ya Pomeranchuk, Dokl. Akad. Nauk SSSR 78, 889(1951)*  
*R. Hagedorn, Nuovo Cim. Suppl. 3, 147(1965)*

$$\varepsilon_\pi = \frac{\pi^2}{30} 3T^4 \propto T^4$$

$$\varepsilon_{QCD} \propto 16 T^4$$

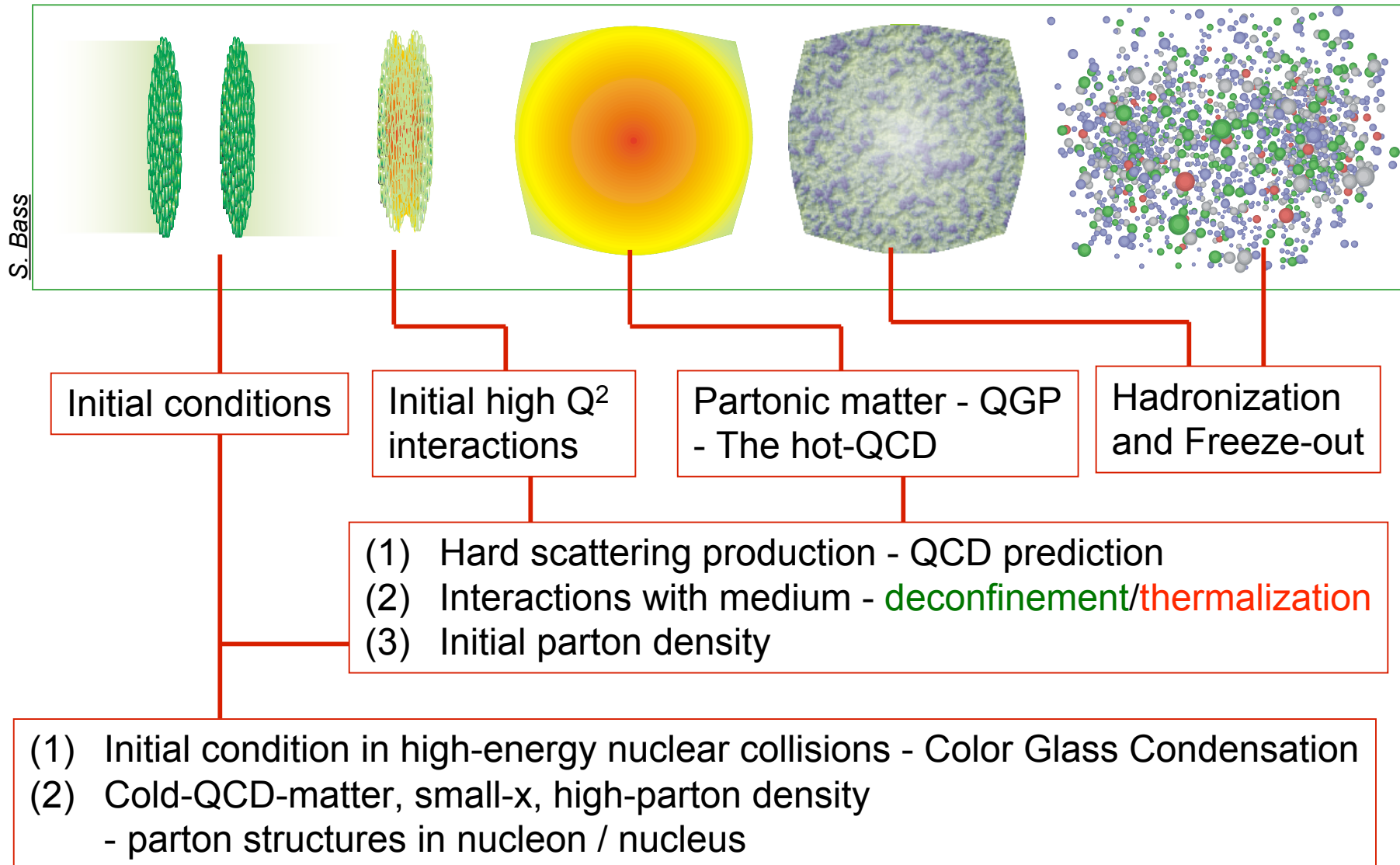
**A large energy density increase for transition from  
hadron to hot quark-gluon system !**







# High-energy Nuclear Collisions



## Initial Condition

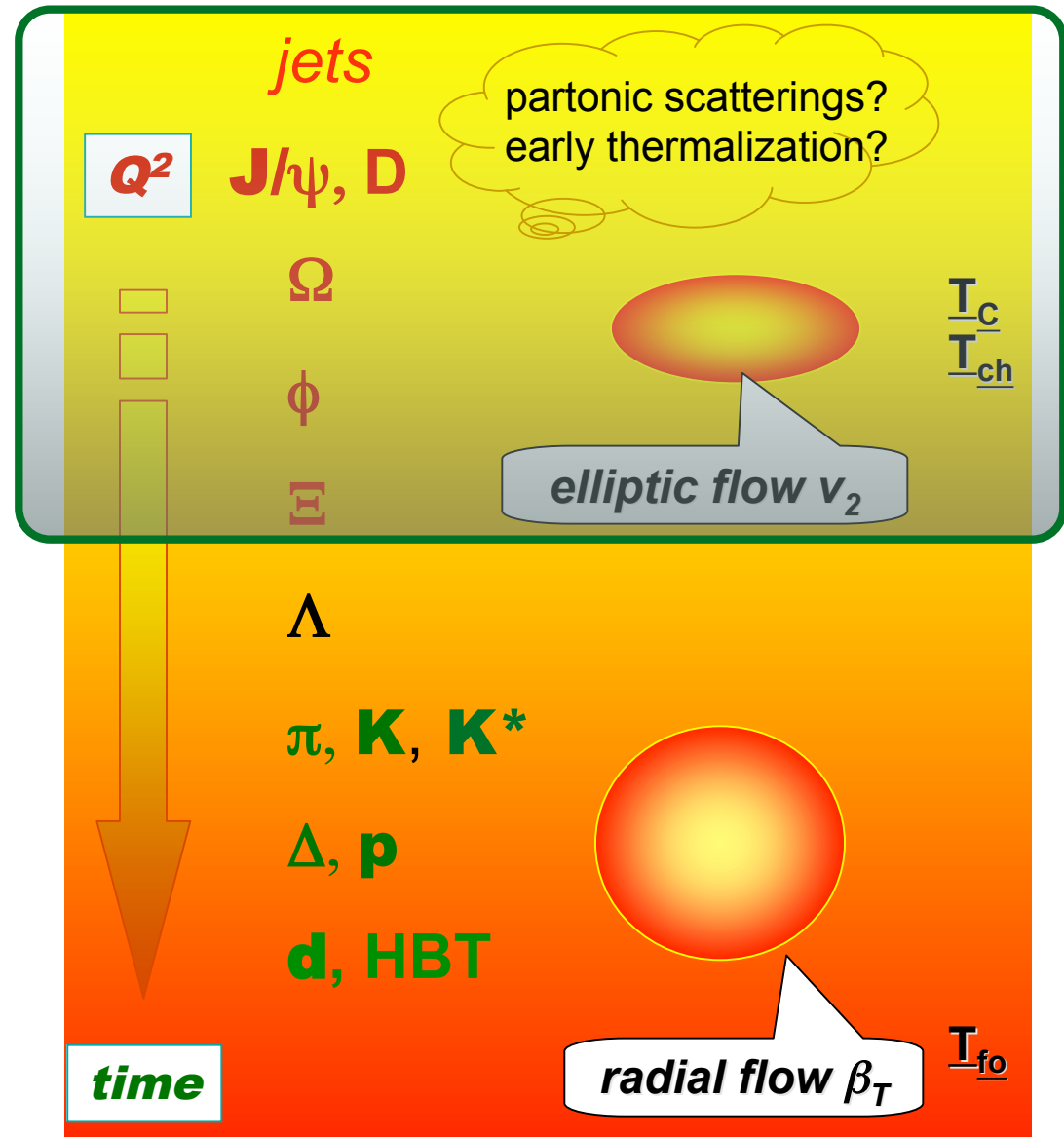
- initial scatterings
- baryon transfer
- $E_T$  production
- parton dof

## System Evolves

- parton interaction
- parton/hadron expansion

## Bulk Freeze-out

- hadron dof
- interactions stop



**Identify and study the properties of matter (EoS) with partonic degrees of freedom and determine the QCD phase diagram.**

**Penetrating probes**

- direct photons, leptons
- “jets” and heavy flavor

**Bulk probes**

- spectra,  $v_1$ ,  $v_2$  ...
- partonic collectivity
- fluctuations

Hydrodynamic  
Flow

=

*Collectivity*

⊗

Local  
Thermalization

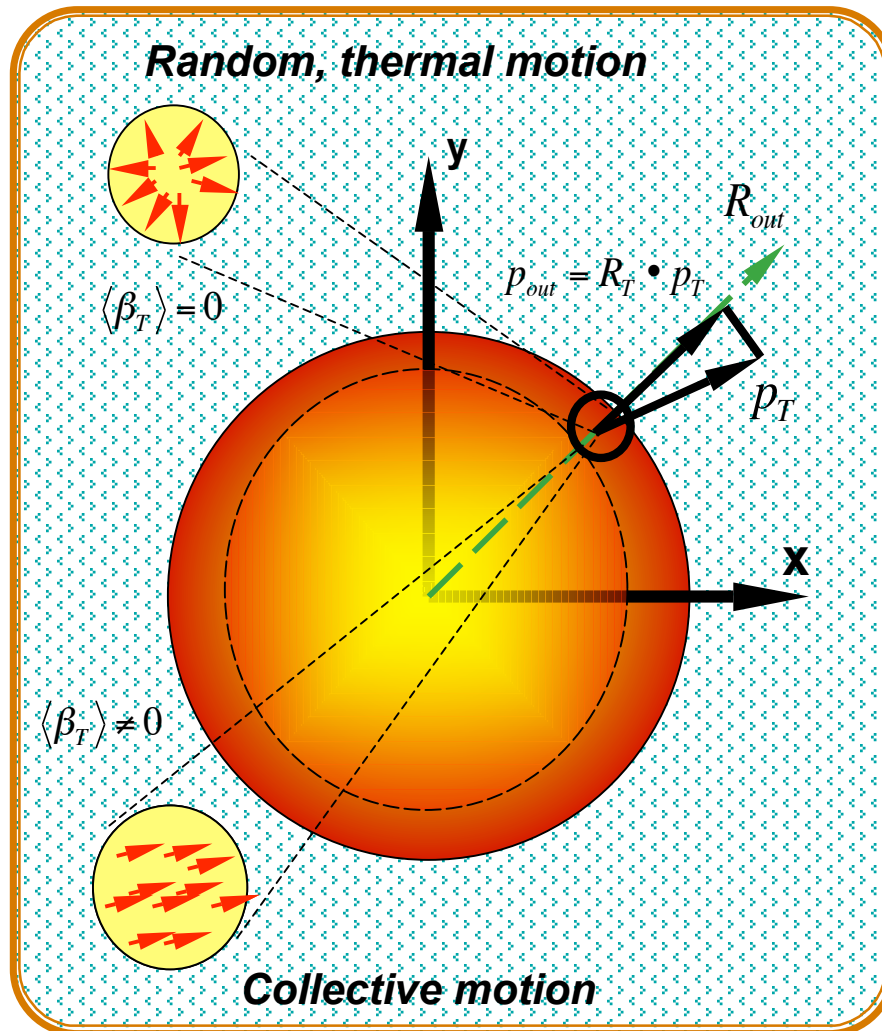
$$\tau d\sigma = dU + p dV$$

$\sigma$  – entropy;  $p$  – pressure;  $U$  – energy;  $V$  – volume  
 $\tau = k_B T$ , thermal energy per dof

In high-energy nuclear collisions, *interaction* among *constituents* and *density distribution* will lead to:

***pressure gradient  $\Leftrightarrow$  collective flow***

- $\Leftrightarrow$  number of degrees of freedom (dof)
- $\Leftrightarrow$  Equation of State (EOS)
- $\Leftrightarrow$  No thermalization is needed – pressure gradient only depends on the ***density gradient and interactions***.
- $\Rightarrow$  Space-time-momentum correlations!



Matter flows – all hadrons have the similar collective velocity

Random  
Thermal

$\oplus$

Collective

$$\langle p_T \rangle \propto \langle p_T \rangle_{thermal} + mass * \langle v_T \rangle$$

$$T \propto T_{thermal} + mass * \langle v_T \rangle^2$$

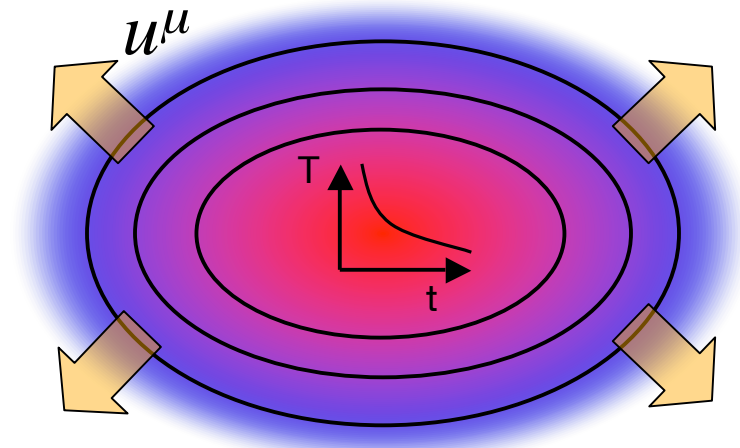
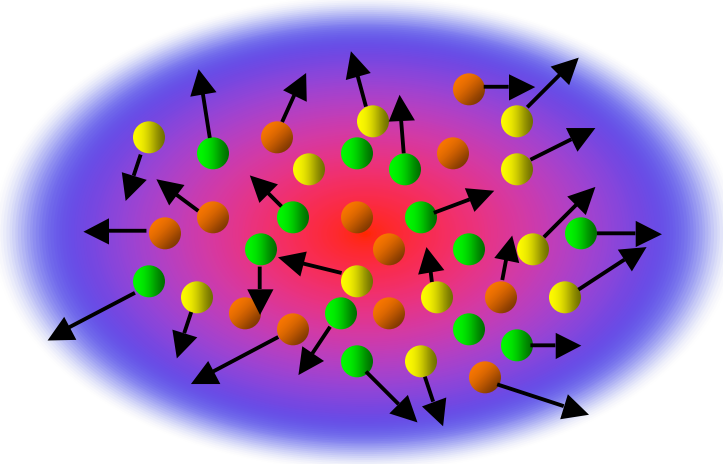
$$\langle p_T \rangle_{thermal} \propto \sqrt{mass * T_{thermal}}$$

I. Bearden et al, Phys. Rev. Lett. **78**, 2080(97).

microscopic view

vs

macroscopic view



scattering rate  $\nu_{ab} \sim$

$$\int \frac{d^3 p_a}{(2\pi)^3} \frac{d^3 p_b}{(2\pi)^3} f_a(p_a) f_b(p_b) \sigma_{ab}(s) |\vec{v}_a - \vec{v}_b|$$

expansion rate  $\partial_\mu u^\mu$

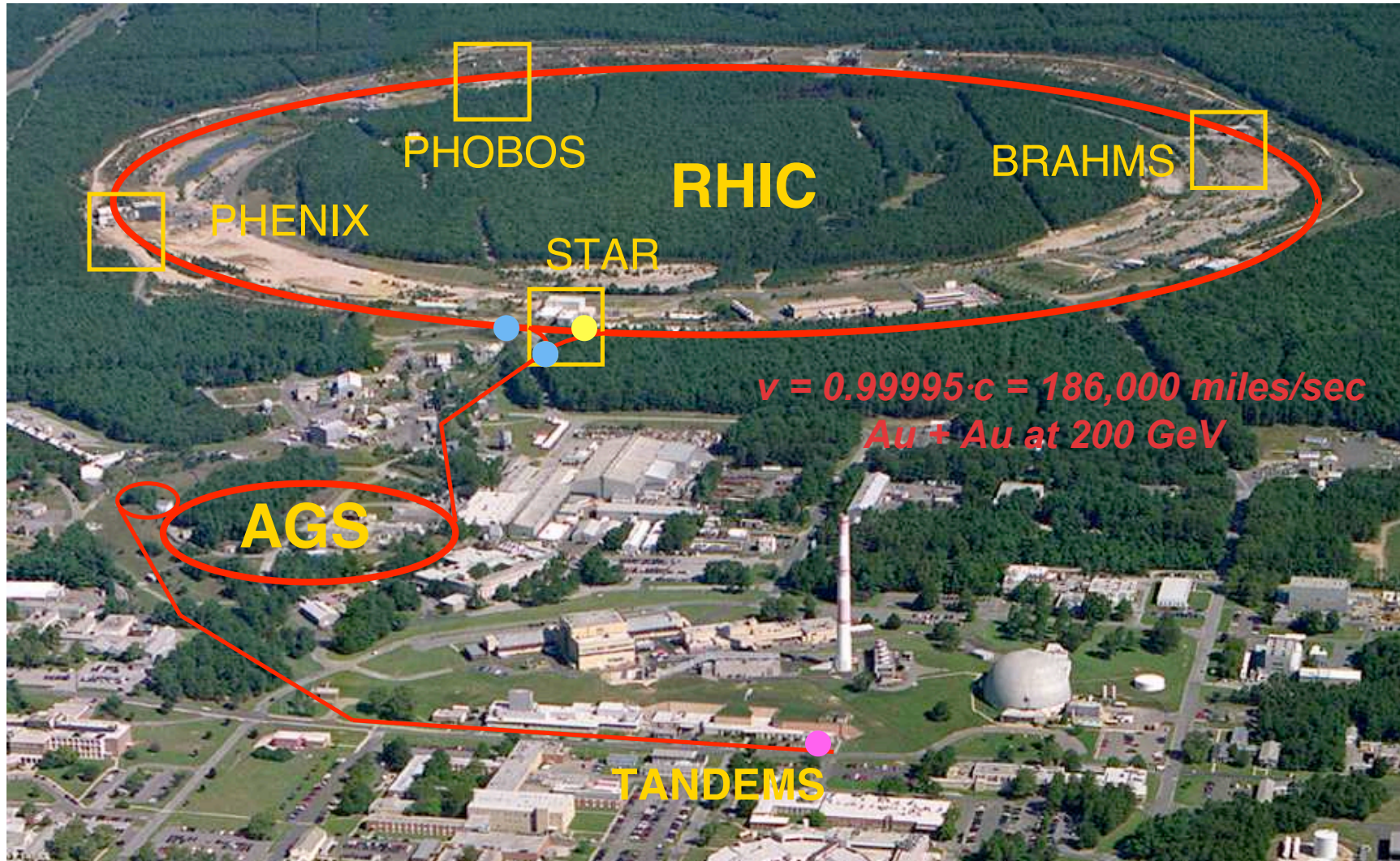
dilution rate  $\partial_\tau s$

A macroscopic treatment requires that the scattering rate is larger than macroscopic rates



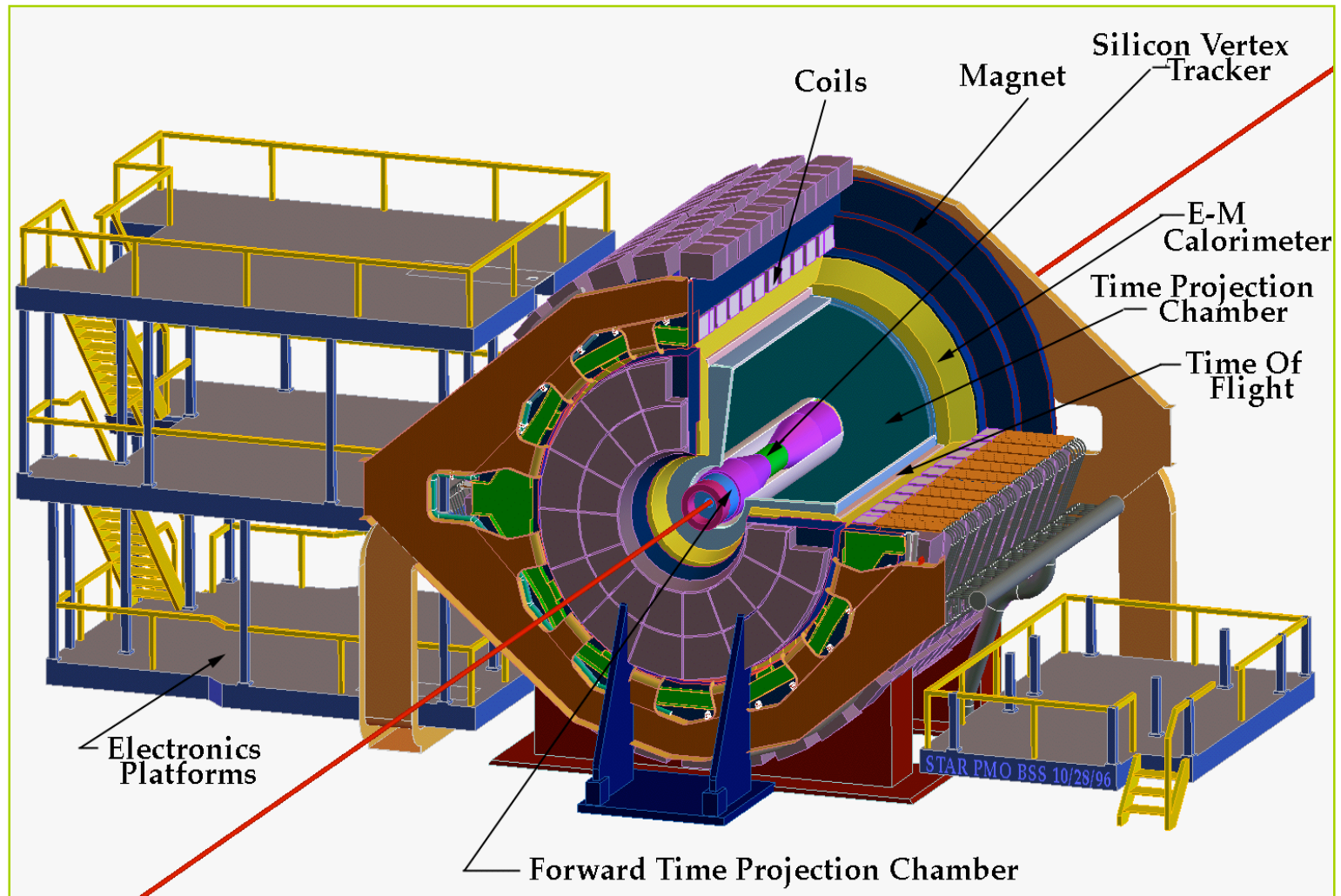
# Relativistic Heavy Ion Collider (RHIC)

Brookhaven National Laboratory (BNL), Upton, NY





# STAR Detectors



**TPC  $dE/dx$  PID:**

pion/kaon:  $p_T \sim 0.6$  GeV/c; proton  $p_T \sim 1.2$  GeV/c



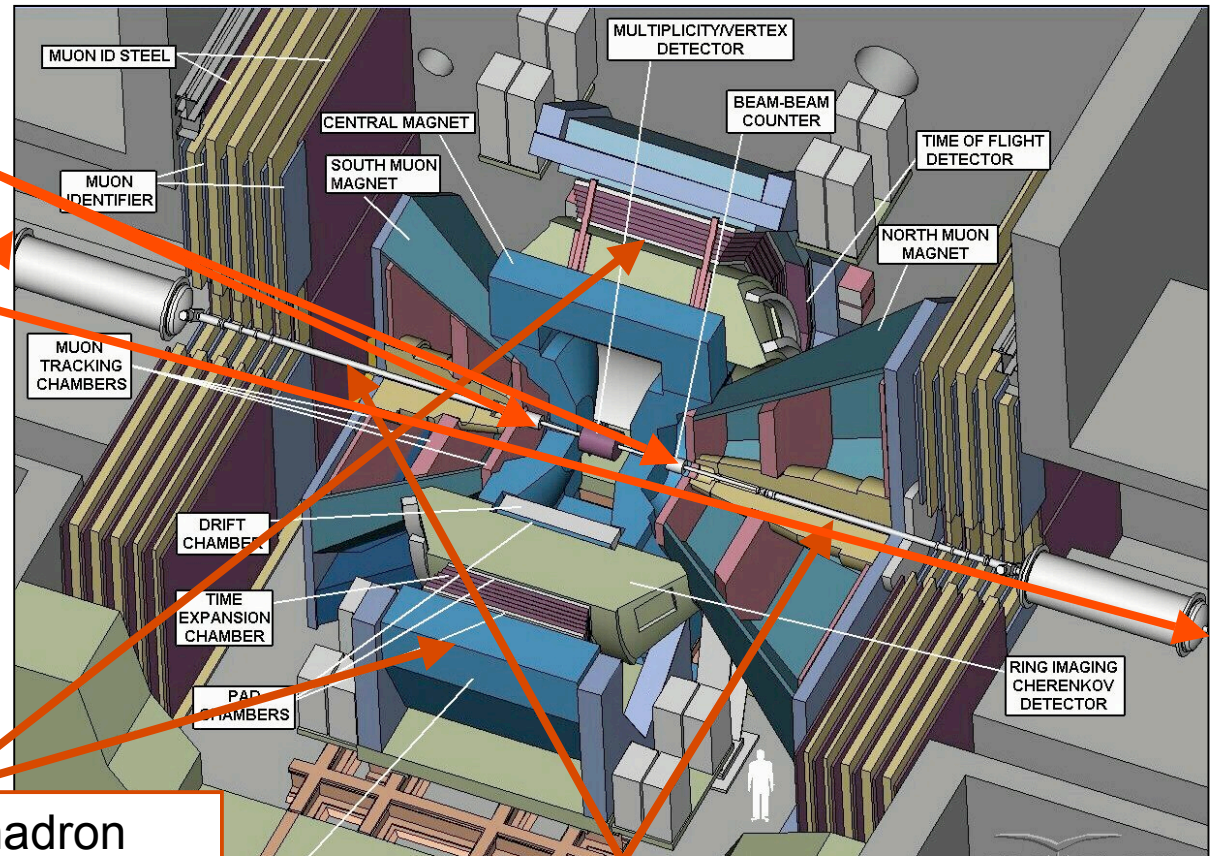
# STAR Collaboration





# PHENIX Detectors

Two sets of forward-rapidity detectors for event characterization  
 Beam-beam counters measure particle production in  $3.0 < |\eta| < 3.9$ .  
 Luminosity monitor + vertex determination.  
 Zero-degree calorimeters measure forward-going neutrons.  
 Correlation gives centrality



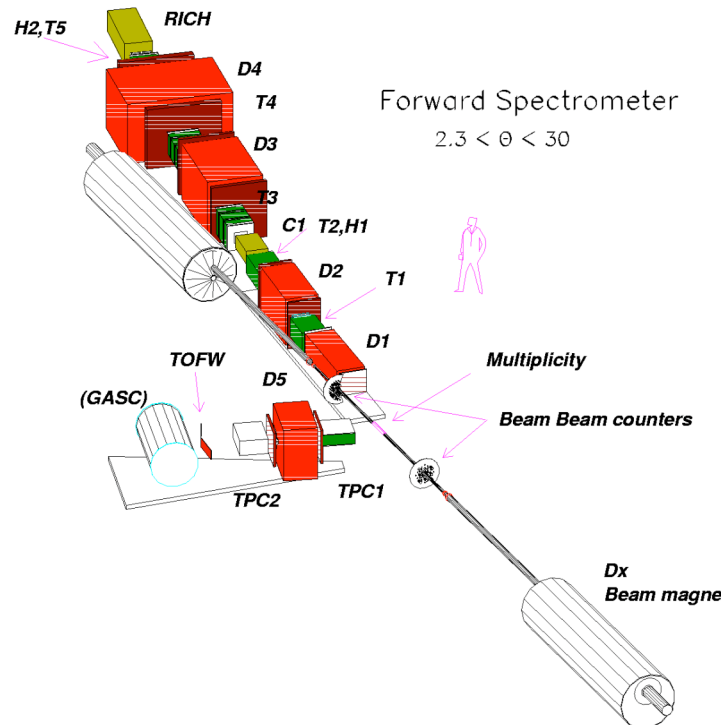
Two central electron/photon/hadron spectrometers:  
 • Tracking, momentum measurement with drift chamber, pixel pad chambers  
 • e ID with E/p ratio in EmCAL + good ring in RICH counter.

Two forward muon spectrometers  
 • Tracking, momentum measurement with cathode strip chambers  
 •  $\mu$  ID with penetration depth / momentum match

# The Two Smaller Detectors

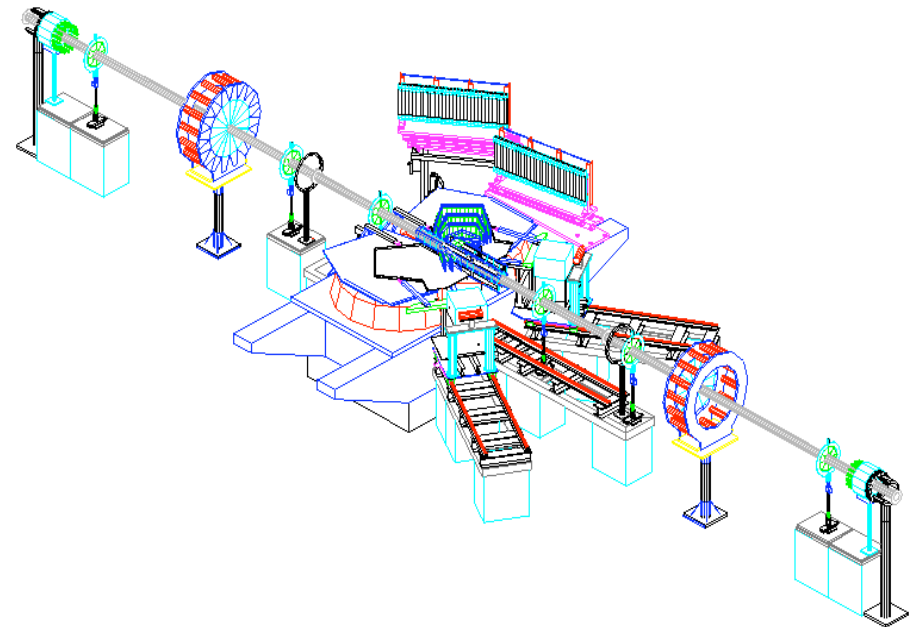
## BRAHMS

2 “conventional” spectrometers  
full phase space coverage  
Magnets, TPCs, TOF, RICH  
~40 participants

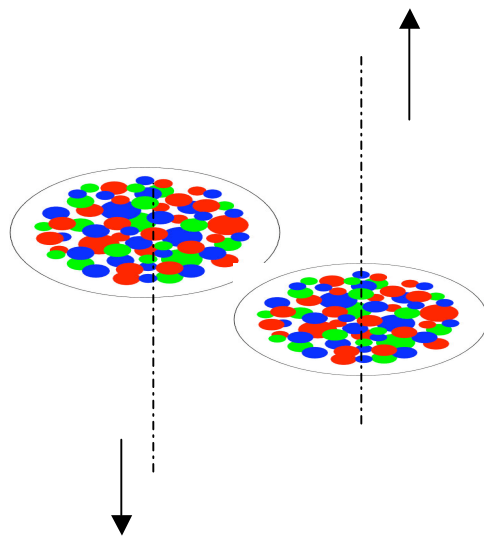


## PHOBOS

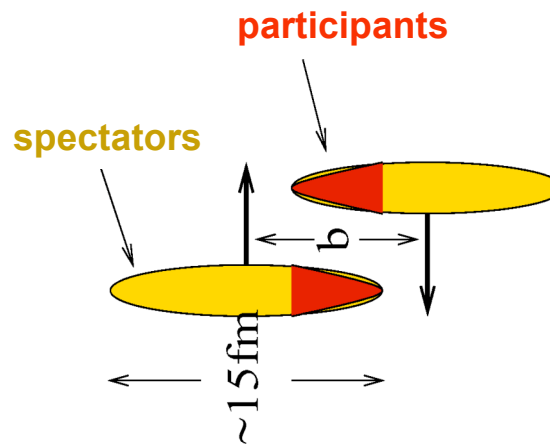
“Table-top” 2-arm spectrometer  
full phase space multiplicity measurement  
Magnet, Si  $\mu$ -strips, Si multiplicity rings, TOF  
~80 participants



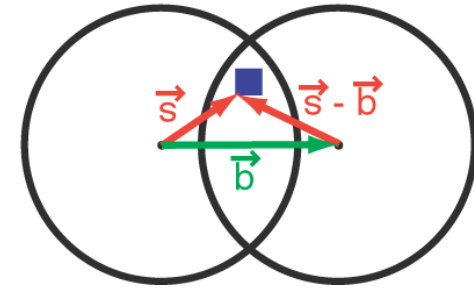
# Collision Geometry



Top-View



$b$ : impact parameter

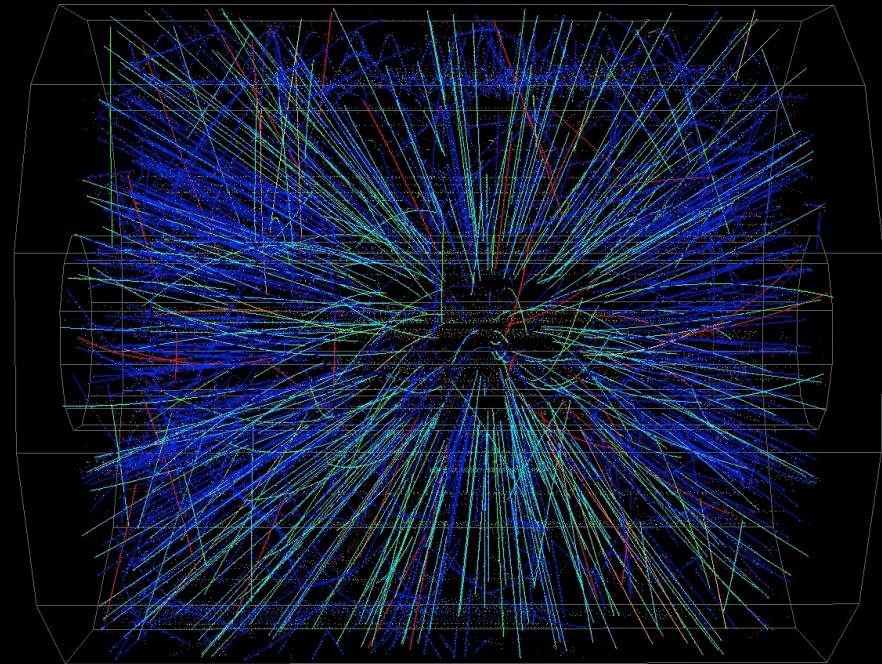
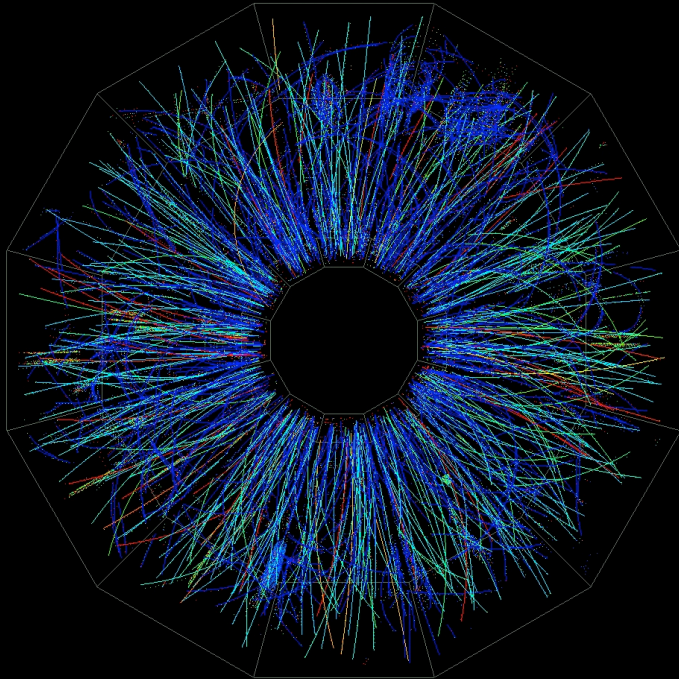


End-View



## *Au + Au Collisions at 130 GeV*

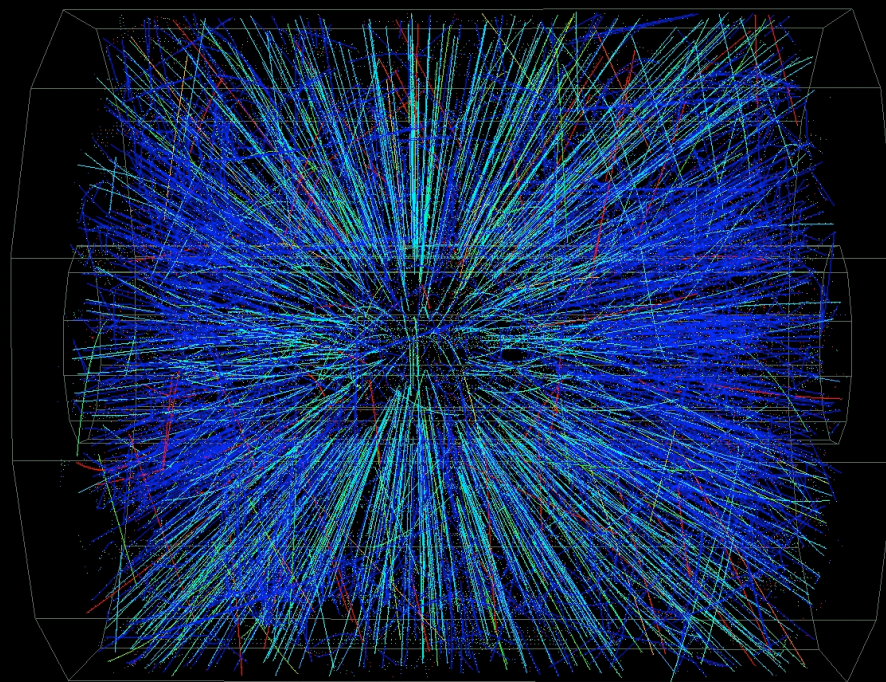
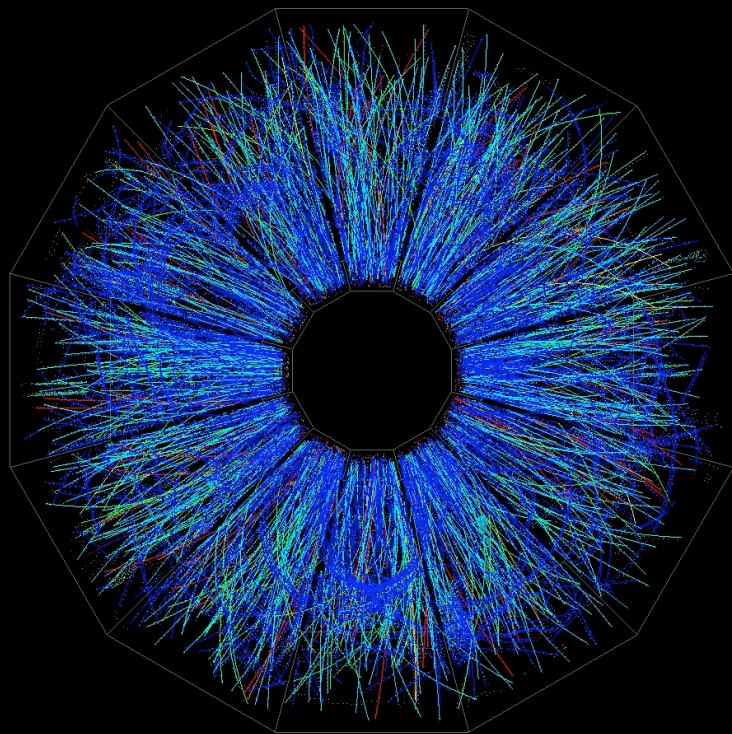
### Peripheral Event



(real-time Level 3)

# *Au + Au Collisions at 130 GeV*

## Mid-Central Event

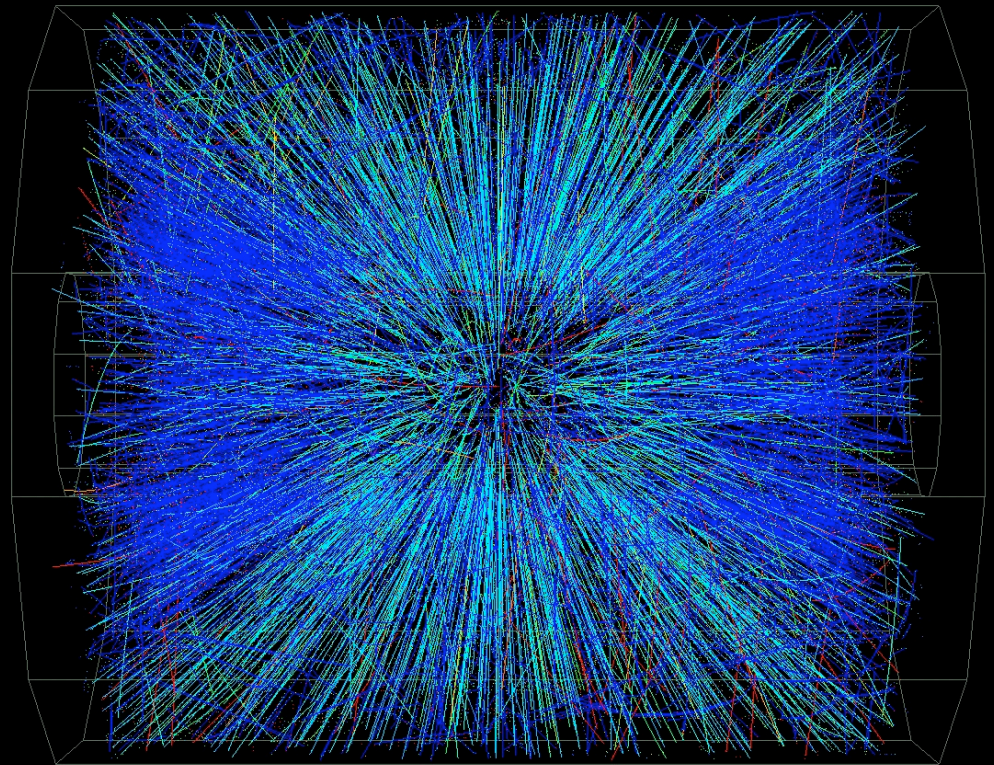
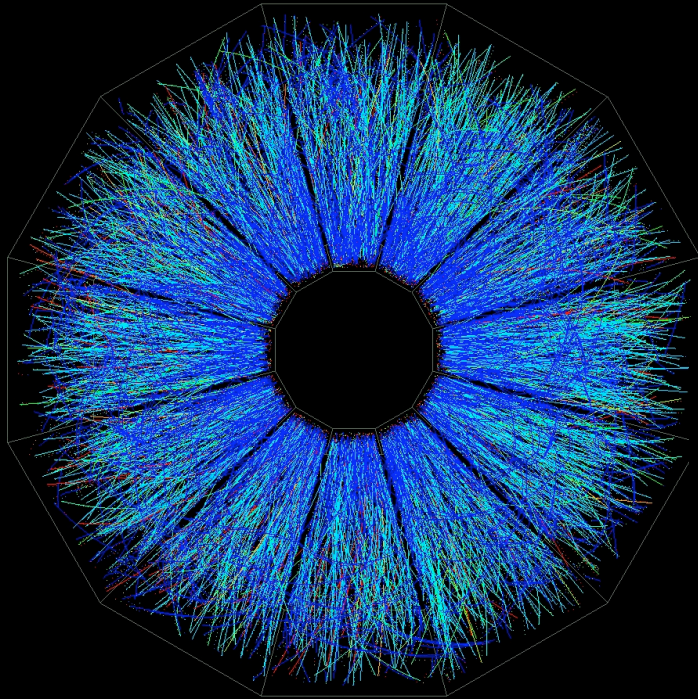


(real-time Level 3)



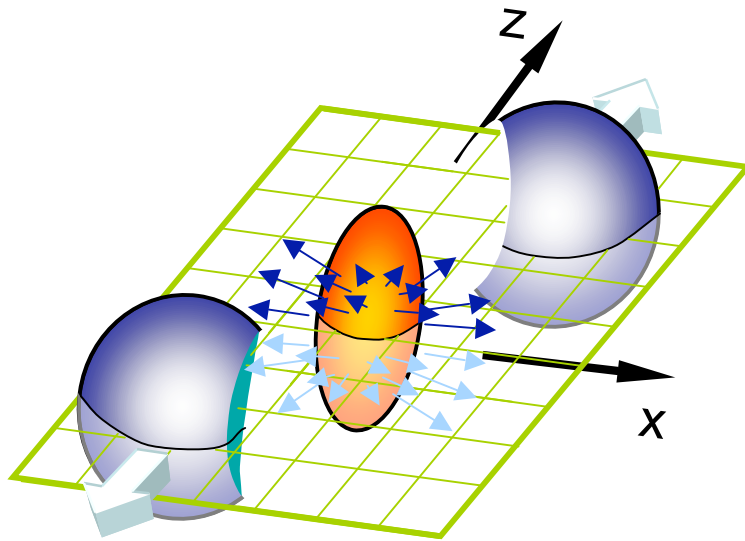
## *Au + Au Collisions at RHIC*

### Central Event

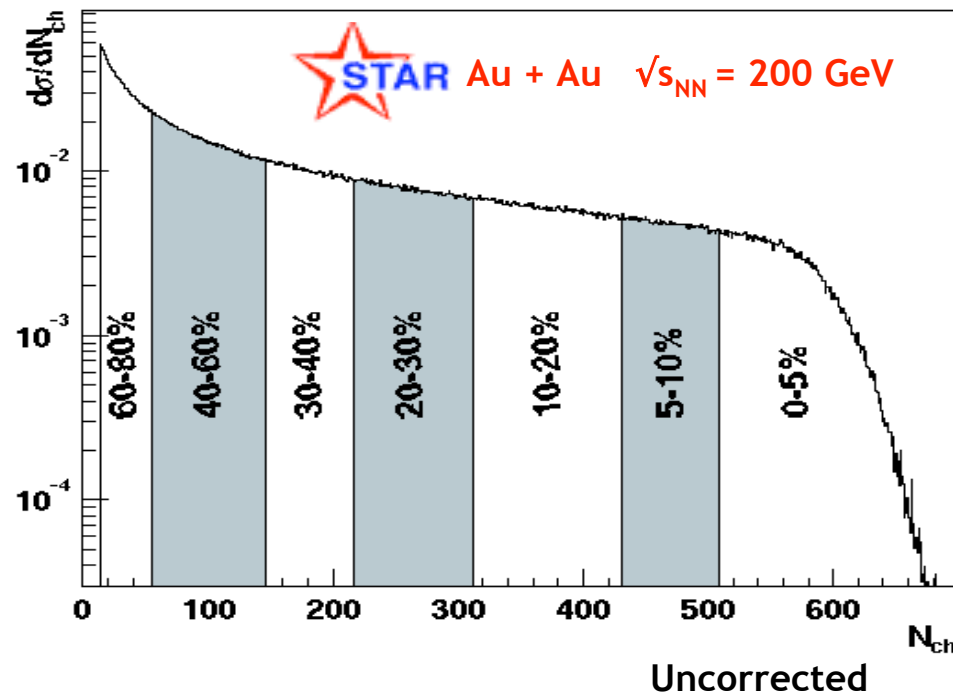


(real-time Level 3)

# Collision Geometry



Non-central Collisions



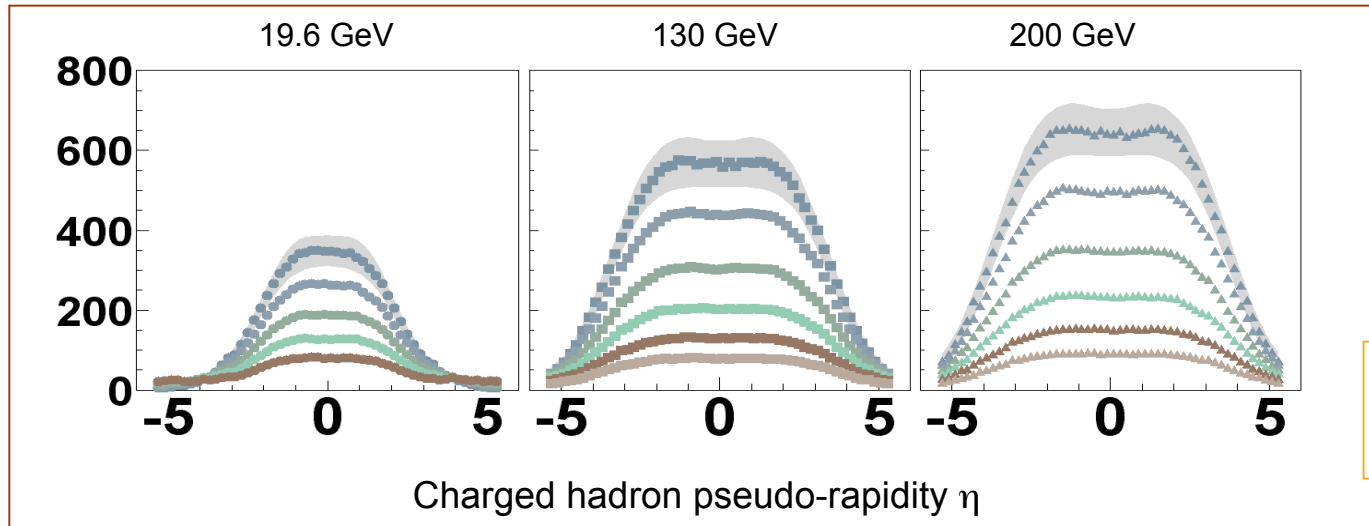
**Number of participants:** number of incoming nucleons in the overlap region

**Number of binary collisions:** number of inelastic nucleon-nucleon collisions

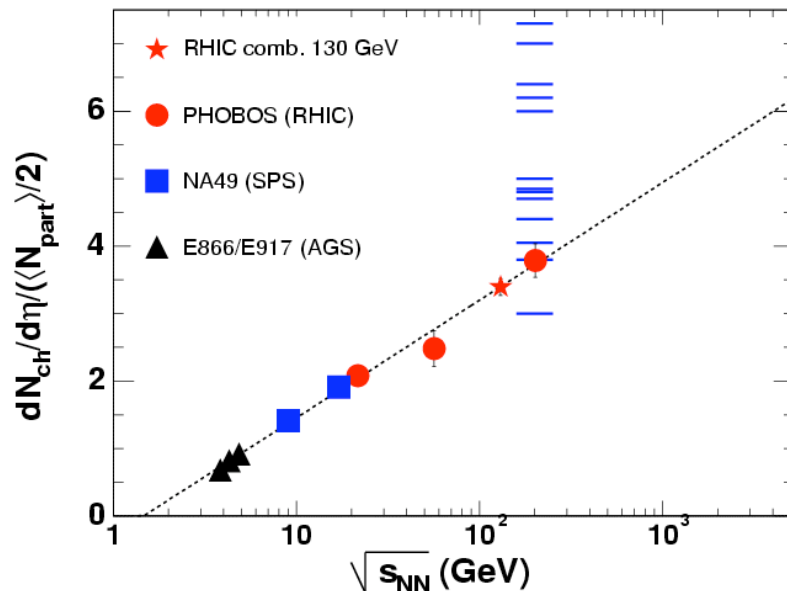
Charged particle multiplicity  $\Leftrightarrow$  collision centrality

Reaction plane: x-z plane





PHOBOS  
Collaboration

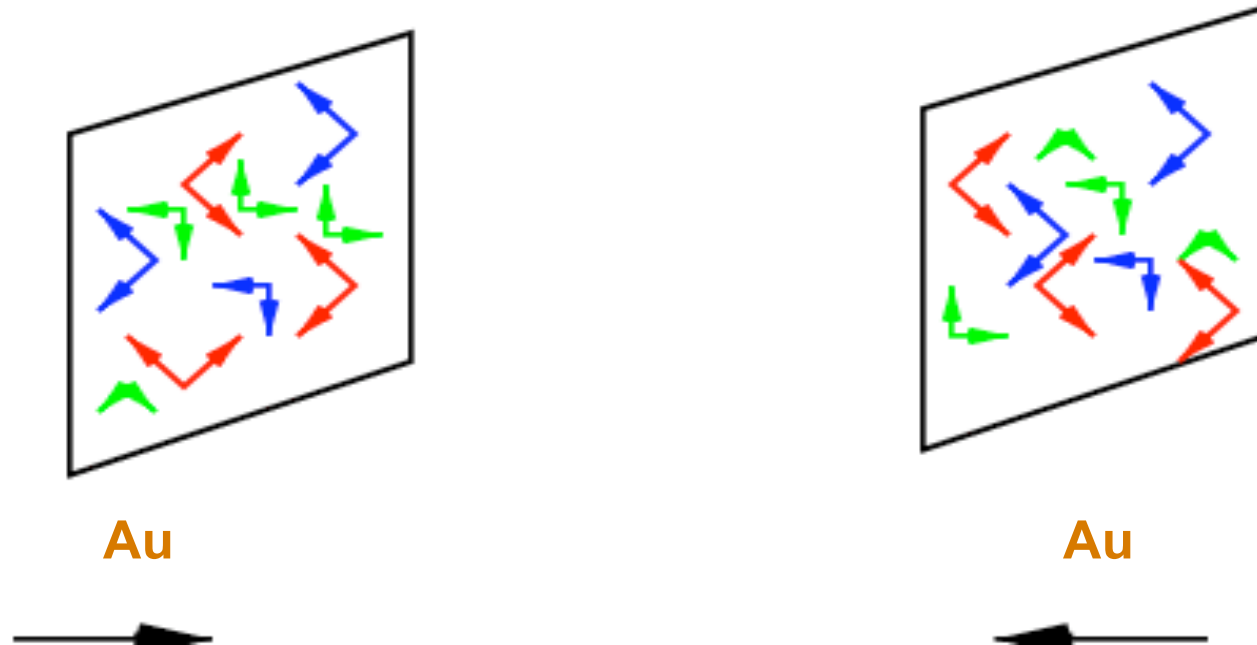


- 1) High number of  $N_{ch}$  indicates initial high density;
- 2) Mid-y,  $N_{ch} \propto N_{part} \Rightarrow$  nuclear collisions are not incoherent;

**Important for high density  
and thermalization.**

PRL **85**, 3100 (00); **91**, 052303 (03); **88**, 22302 (02), **91**, 052303 (03)

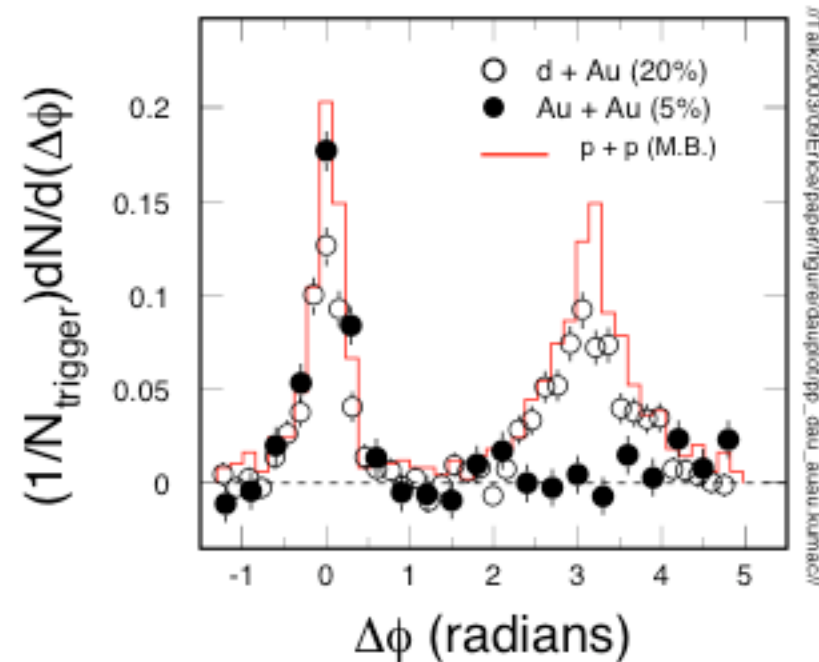
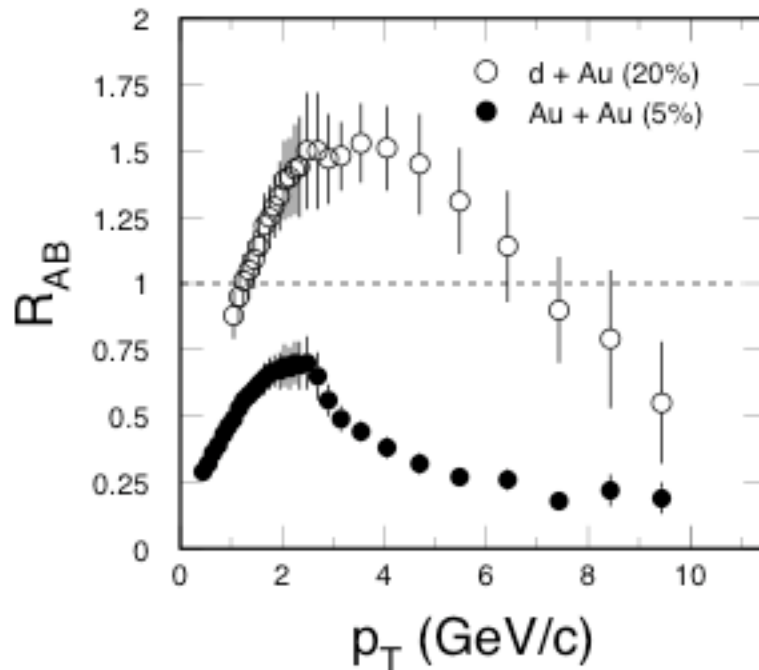
# Color Glass Condensate



Random Electric & Magnetic Weizsacker-Williams fields in the plane of the fast moving nucleus

A possible state for the initial conditions at RHIC

# Suppression and Correlation



In central Au+Au collisions: hadrons are suppressed and back-to-back ‘jets’ are disappeared. Different from p+p and d+Au collisions.

Energy density at RHIC:  $\epsilon > 5 \text{ GeV/fm}^3 \sim 30\epsilon_0$

Parton energy loss:  
 (“**Jet quenching**”)

Bjorken

1982

Gyulassy & Wang

1992

...

# Transverse Flow Observables

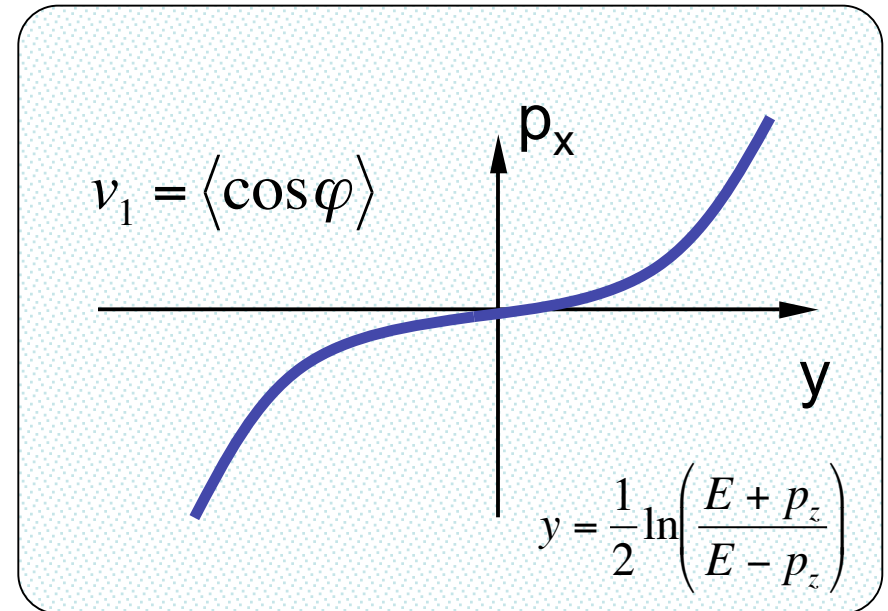
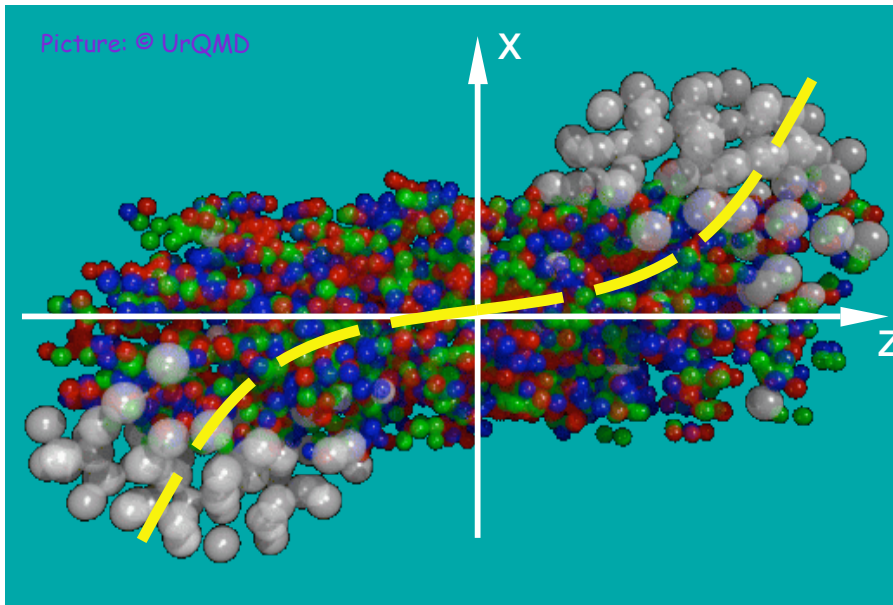
$$\frac{d\vec{\sigma}}{d\Omega} = \frac{d^3\sigma}{dp_x dp_y dp_z} = \frac{dN}{p_t dp_t dy d\varphi} = \frac{1}{2\pi} \frac{dN}{p_t dp_t dy} \left[ 1 + \sum_{i=1} 2v_i \cos(i\varphi) \right]$$

$$p_t = \sqrt{p_x^2 + p_y^2}, \quad m_t = \sqrt{p_t^2 + m^2}$$

$$v_i = \langle \cos(i\varphi) \rangle_{event} \quad \varphi = \tan^{-1} \left( \frac{p_y}{p_x} \right)$$

- 1) Radial flow – integrated over whole period of evolution
  - 2) Directed flow ( $v_1$ ) – relatively early
  - 3) Elliptic flow ( $v_2$ ) – relatively early
- Hadron mass dependent: characteristic of hydrodynamic behavior.

# Directed Flow $v_1$



Initial spatial anisotropy

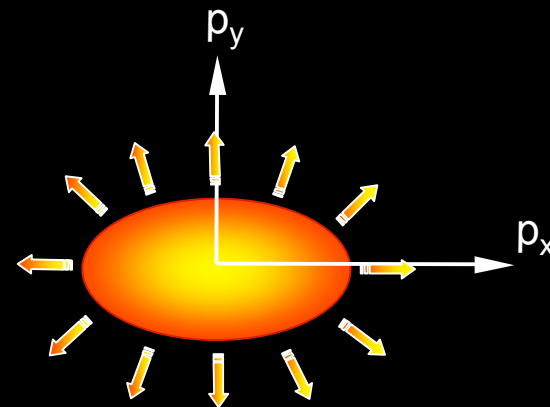
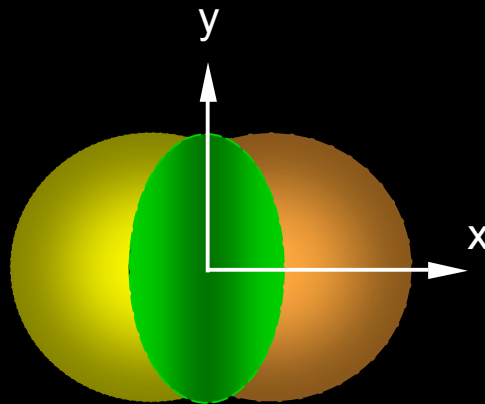


Anisotropy in momentum space

coordinate-space-anisotropy



momentum-space-anisotropy

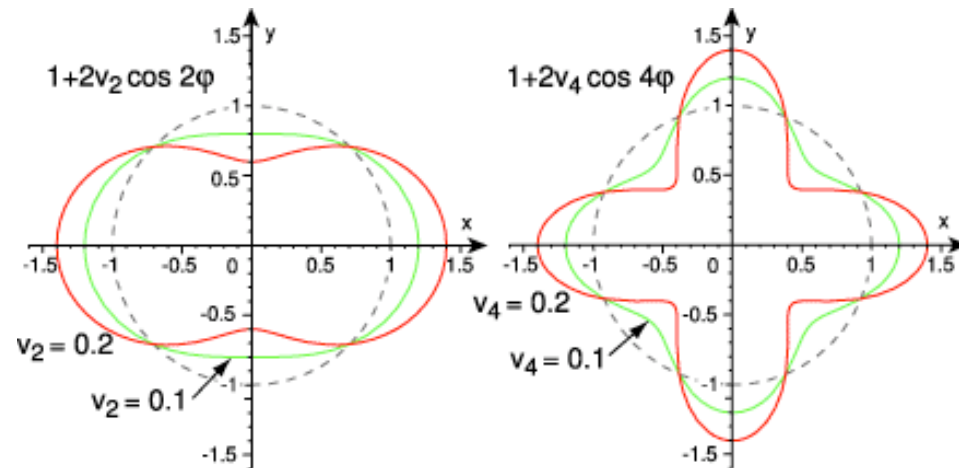
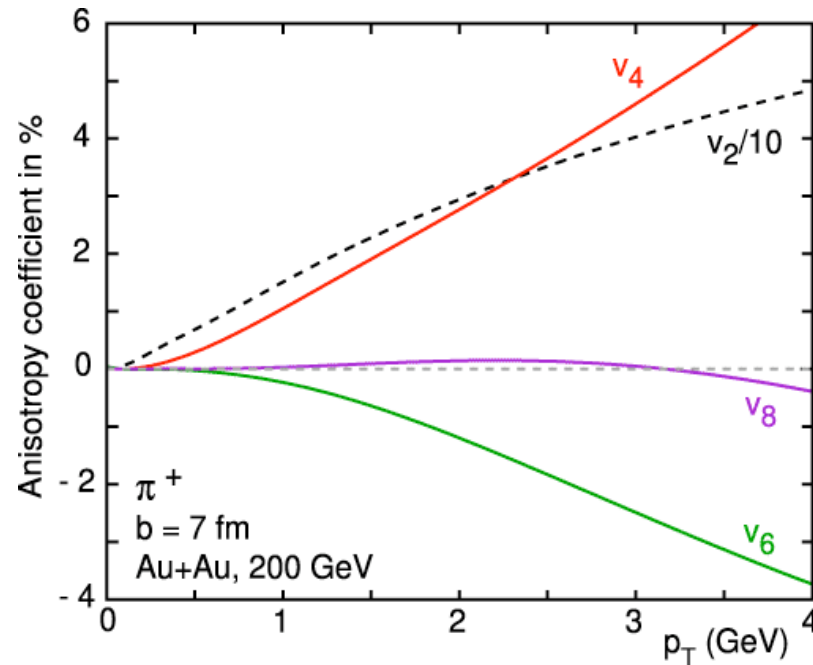


$$\varepsilon = \frac{\langle y^2 - x^2 \rangle}{\langle y^2 + x^2 \rangle}$$

$$v_2 = \langle \cos 2\varphi \rangle, \quad \varphi = \tan^{-1}\left(\frac{p_y}{p_x}\right)$$

**Initial/final conditions, EoS, degrees of freedom**

# Higher Harmonics



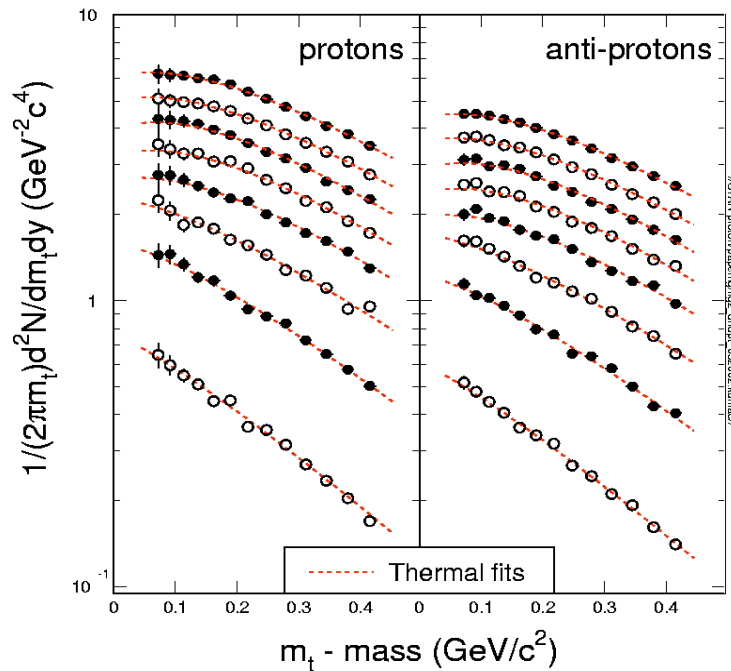
Peter Kolb, PRC 68, 031902

- Higher harmonics are expected to be present. For smooth azimuthal distributions the higher harmonics will be small  $v_n \sim v_2^{n/2}$
- $v_4$  - a small, but sensitive observable for heavy ion collisions.
- $v_4$  - magnitude sensitive to ideal hydro behavior.

P. Kolb, PR C68, 031902(04)

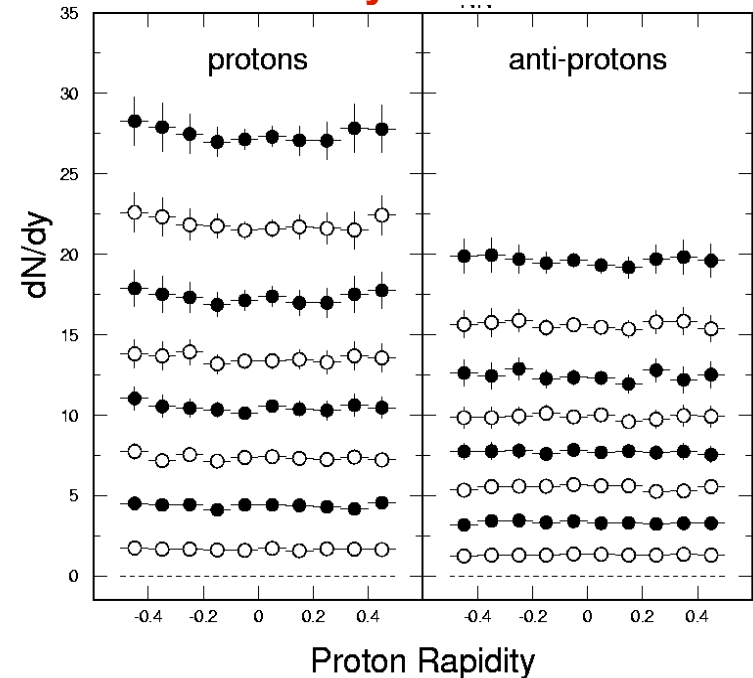
Borghini and Ollitrault, nucl-th/0506045

K. Schweda, M. Kaneta ...



More central collisions

**130 GeV Au + Au Collisions**  
**STAR Preliminary**

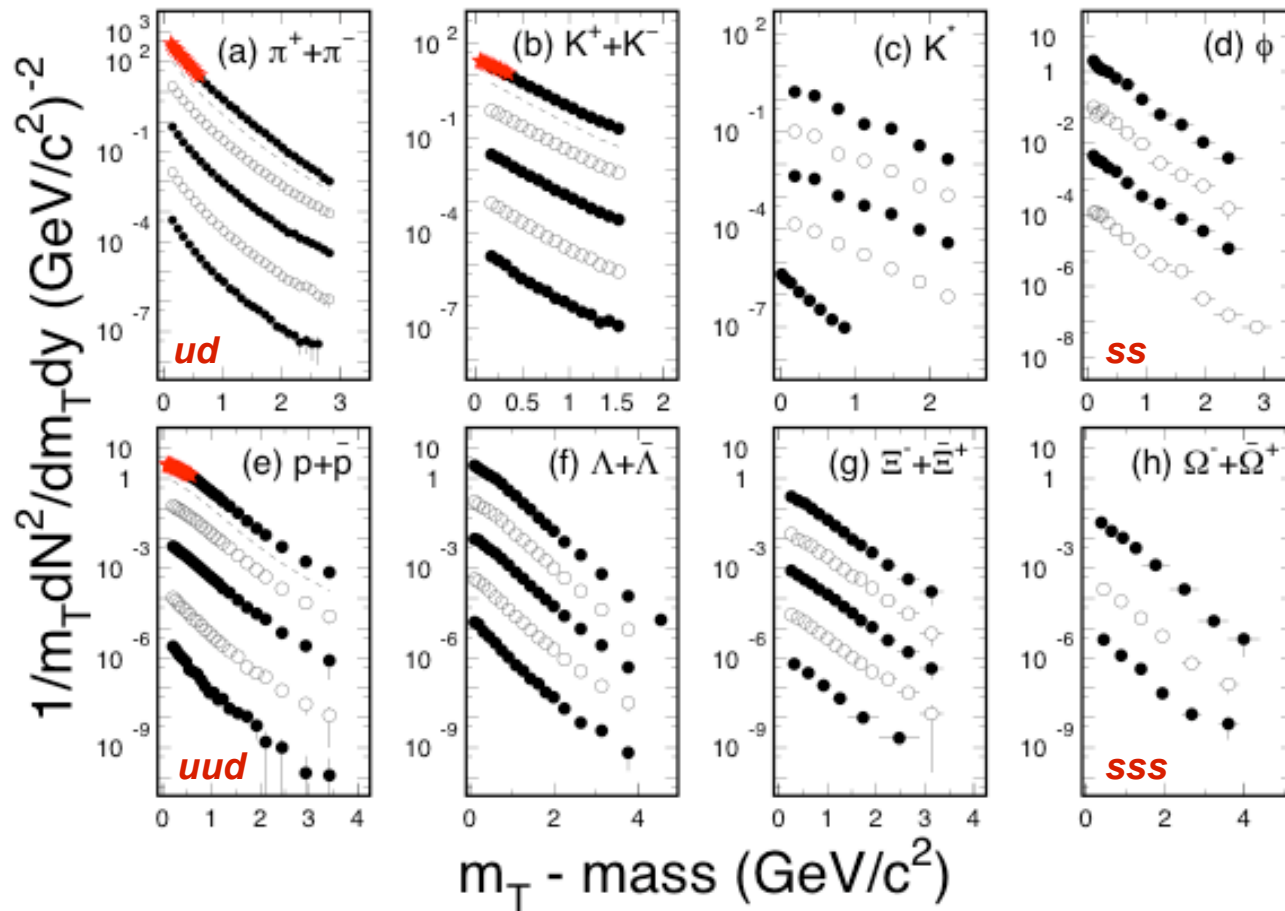


- 1) In central collisions,  $m_t$  distributions become more concave  $\Rightarrow$  collective flow !
- 2) Within  $|y| < 0.5$ ,  $dN/dy$  and  $\langle p_T \rangle$  are flat  $\Rightarrow$  boost invariant !



# Hadron Spectra from RHIC

*p+p and Au+Au collisions at 200 GeV*



more central collisions  
↑  
0-5%

$$m_T = \sqrt{p_T^2 + m^2}$$

$$f \propto \exp(-m_T/T_{\text{slope}})$$

**Multi-strange hadron spectra are exponential in their shapes.**

STAR white papers - Nucl. Phys. A757, 102(2005).

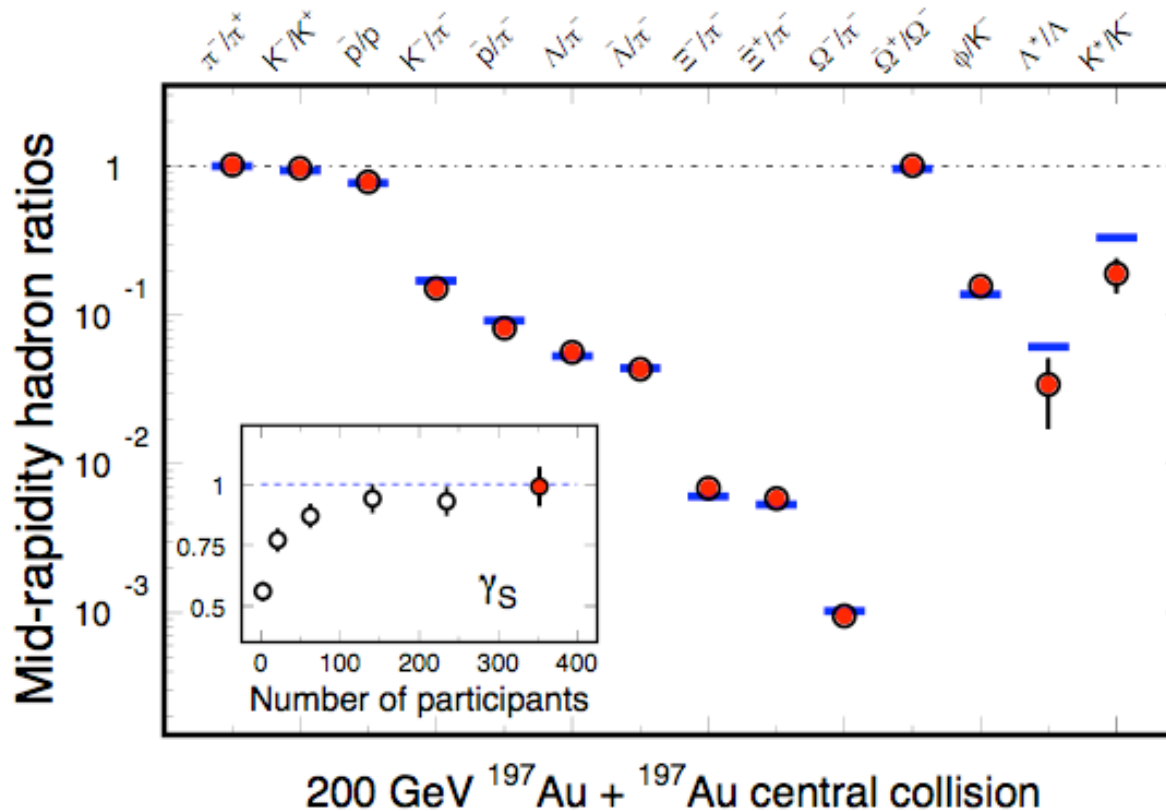
# The Basic Ideas

- Assume thermally (constant  $T_{\text{ch}}$ ) and chemically (constant  $n_i$ ) equilibrated system at chemical freeze-out
- System composed of non-interacting hadrons and resonances
- Given  $T_{\text{ch}}$  and  $m$ 's (+ system size),  $n_i$ 's can be calculated in a grand canonical ensemble

$$n_i = \frac{g}{2\pi^2} \int_0^\infty \frac{p^2 dp}{e^{(E_i(p) - \mu_i)/T} \pm 1}, \quad E_i = \sqrt{p^2 + m_i^2}$$

- Obey conservation laws: Baryon Number, Strangeness, Isospin
- Short-lived particles and resonances need to be taken into account

# Yields Ratio Results



○ data

— Thermal  
model fits

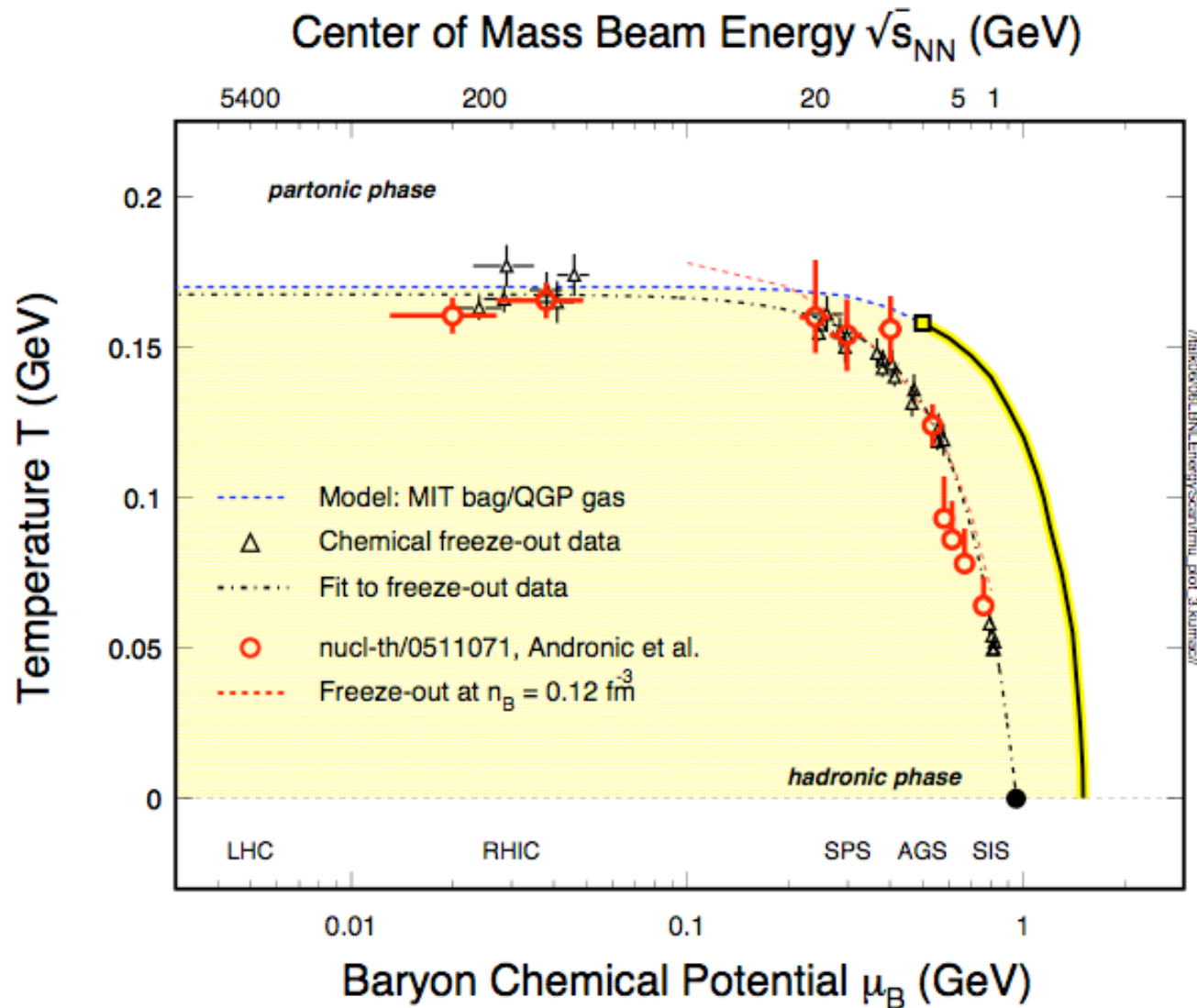
$$T_{\text{ch}} = 163 \pm 4 \text{ MeV}$$

$$\mu_B = 24 \pm 4 \text{ MeV}$$

- In central collisions, thermal model fit well with  $\gamma_S = 1$ . **The system is thermalized at RHIC.**
- Short-lived resonances show deviations. **There is life after chemical freeze-out.**

RHIC white papers - 2005, Nucl. Phys. A757, STAR: p102; PHENIX: p184.

# QCD Phase Diagram



# Thermal Model Fits (Blast-Wave)

Source is assumed to be:

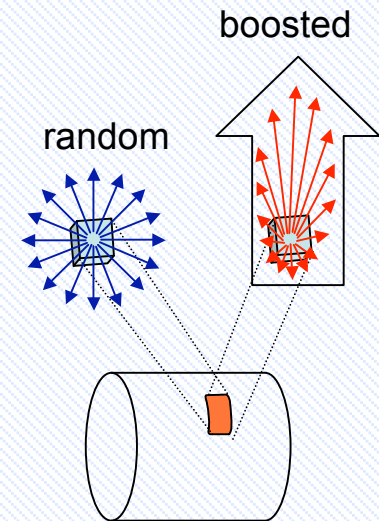
- Locally thermal equilibrated
- Boosted in radial direction

*E. Schnedermann, J. Sollfrank, and U. Heinz, Phys. Rev. **C48**, 2462(1993)*

$$E \frac{d^3 N}{dp^3} \propto \int_{\sigma} e^{-(u^\mu p_\mu)/T_{fo}} p d\sigma_\mu \Rightarrow$$

$$\frac{dN}{m_T dm_T} \propto \int_0^R r dr m_T K_1 \left( \frac{m_T \cosh \rho}{T_{fo}} \right) I_0 \left( \frac{p_T \sinh \rho}{T_{fo}} \right)$$

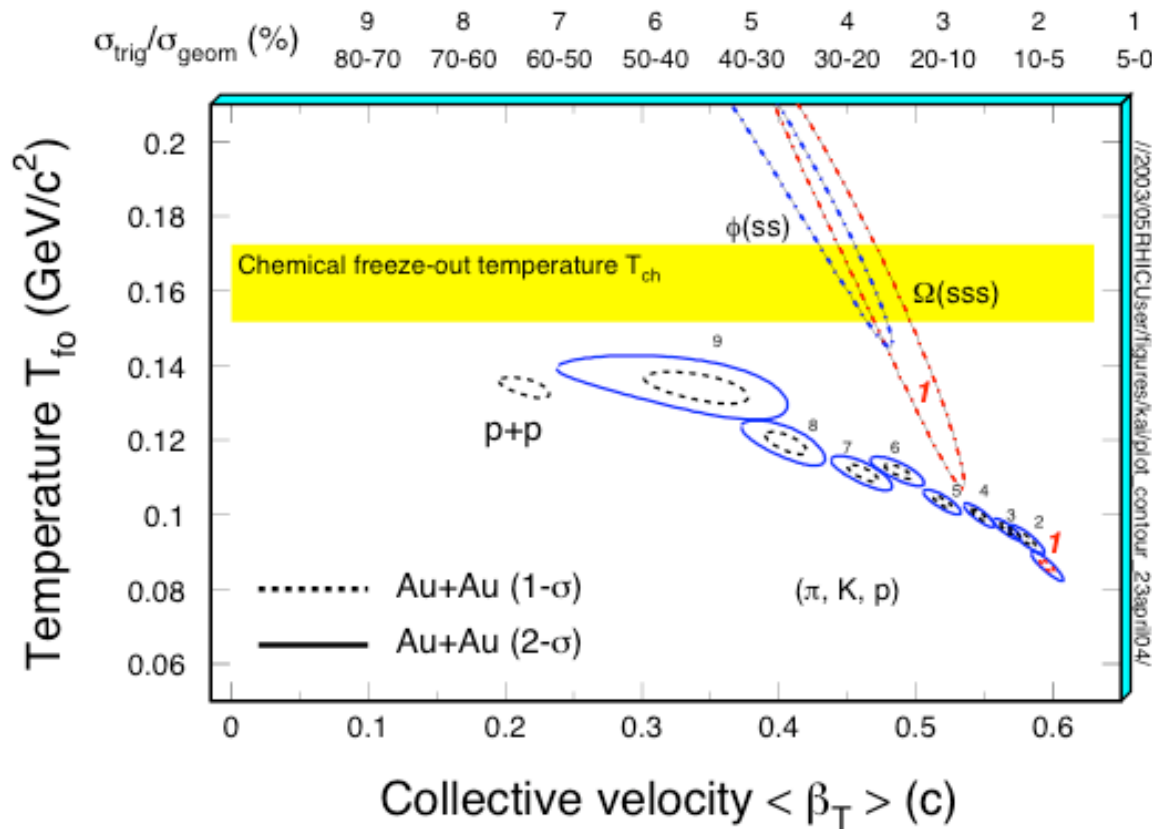
$$\rho = \tanh^{-1} \beta_T \quad \beta_T = \beta_s \left( \frac{r}{R} \right)^\alpha \quad \alpha = 0.5, 1, 2$$



Extract thermal temperature  $T_{fo}$  and velocity parameter  $\langle \beta_T \rangle$

# Blast Wave Fits: $T_{fo}$ vs. $\langle \beta_T \rangle$

## 200GeV Au + Au collisions



1)  $\pi$ ,  $K$ , and  $p$  change smoothly from peripheral to central collisions.

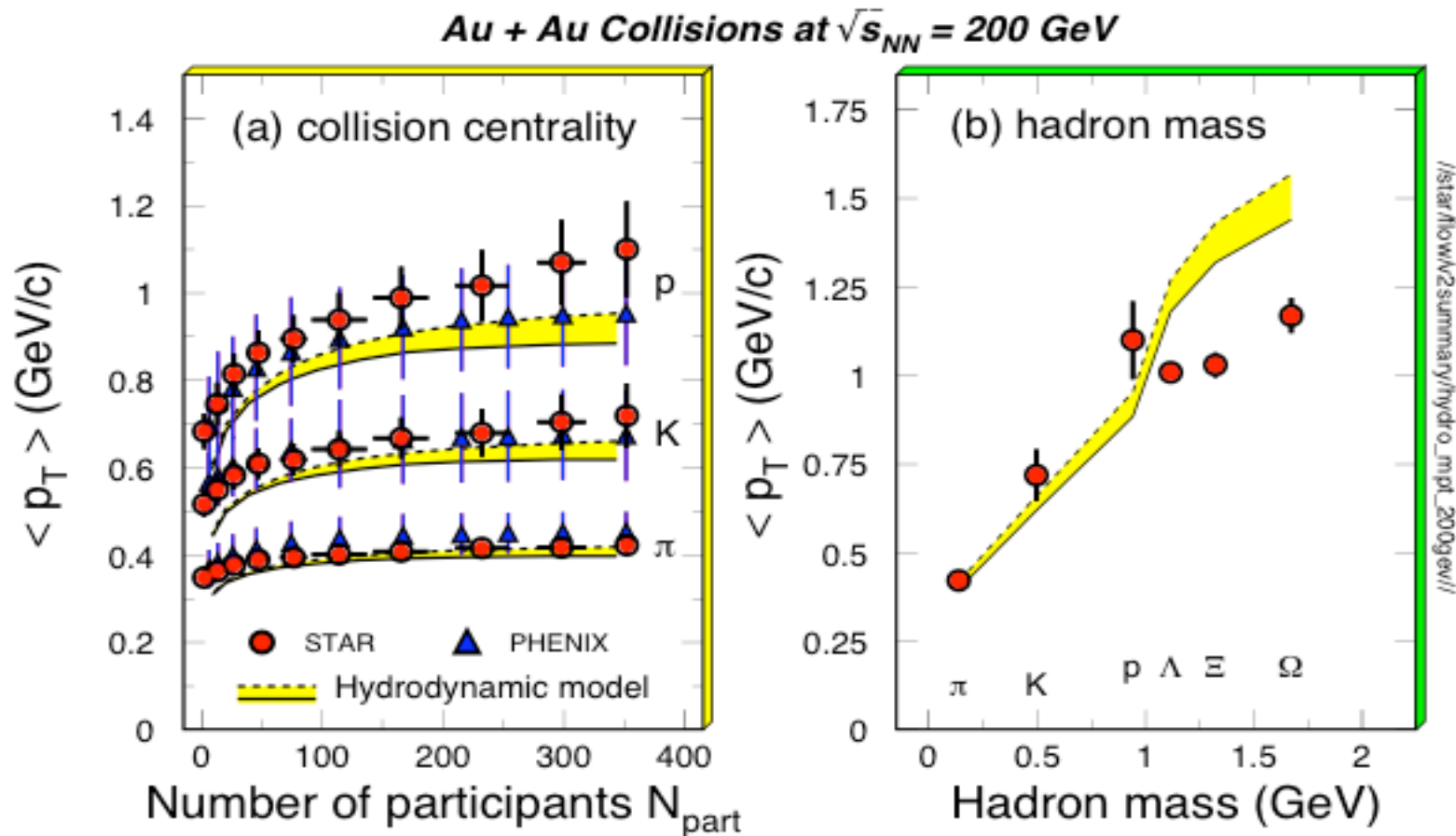
2) At the most central collisions,  $\langle \beta_T \rangle$  reaches 0.6c.

3) Multi-strange particles  $\phi$ ,  $\Omega$  are found at higher  $T_{fo}$  and lower  $\langle \beta_T \rangle$

**⇒ light hadrons move with higher velocity compared to strange hadrons**

STAR: NPA**715**, 458c(03); PRL **92**, 112301(04); **92**, 182301(04).

# Compare with Model Results

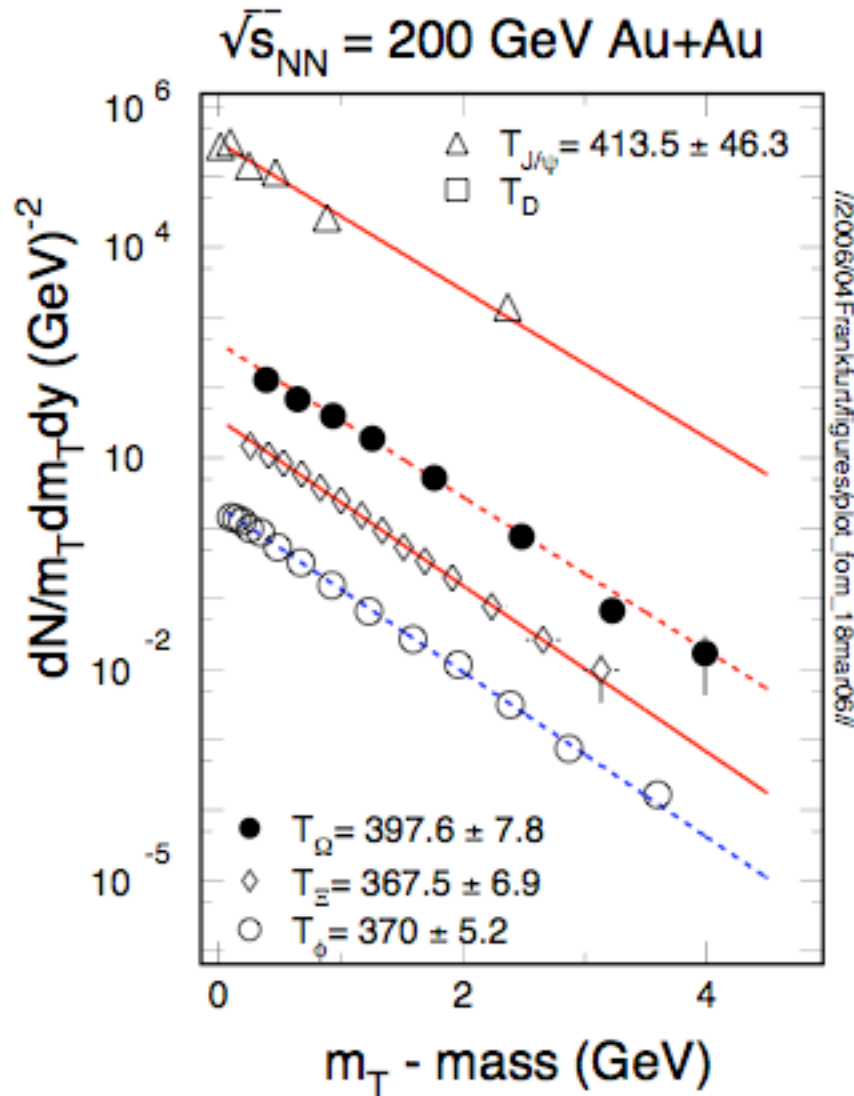


Hydro model works well for  $\pi$ ,  $K$ ,  $p$ , but over-predicts flow for multi-strange hadrons

Initial 'collective kick' introduced (P. Kolb and R. Rapp, PRC67)

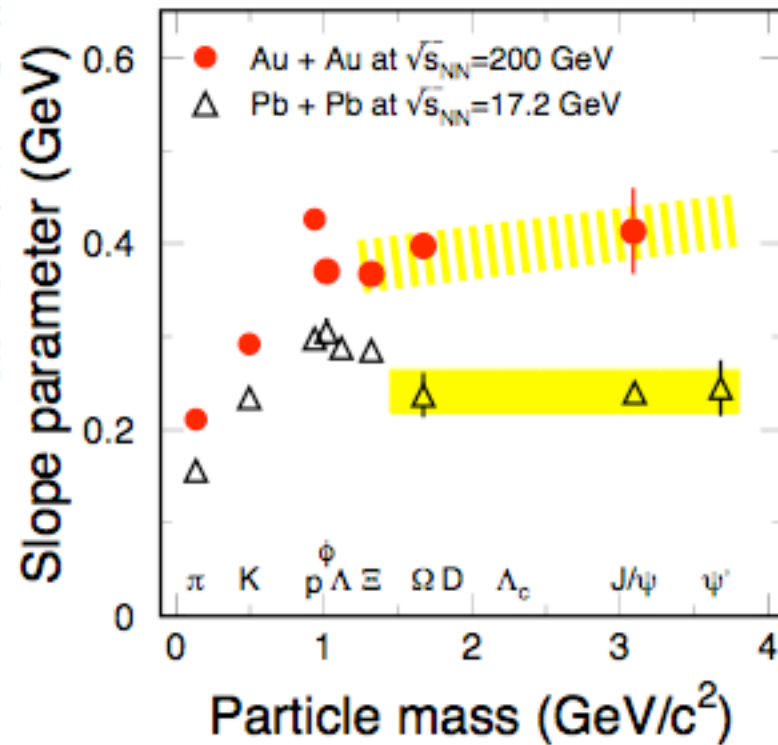


# Slope Parameter Systematics



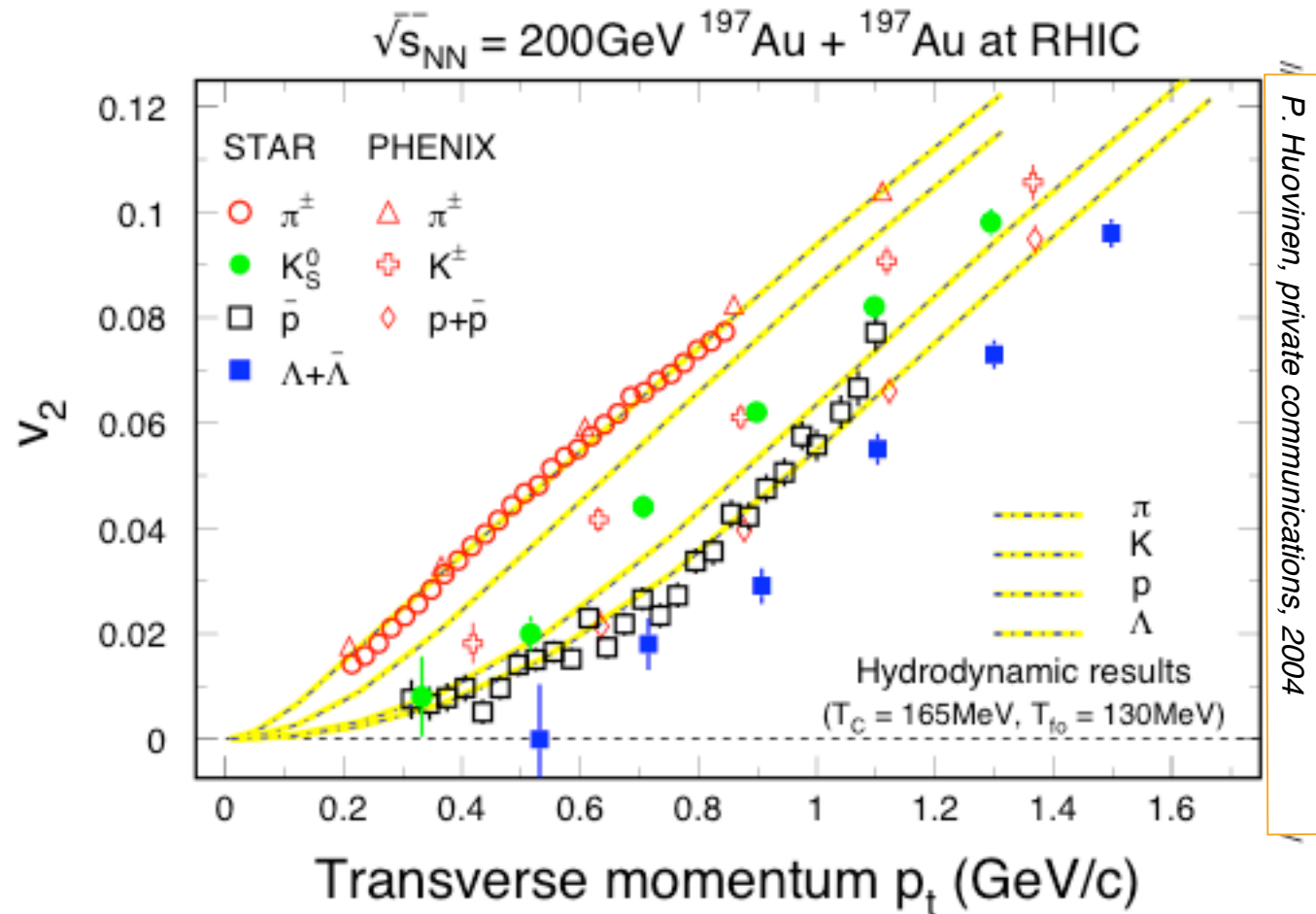
$$m_T = \sqrt{p_T^2 + m^2}$$

$$f \propto \exp(-m_T/T_{\text{slope}})$$



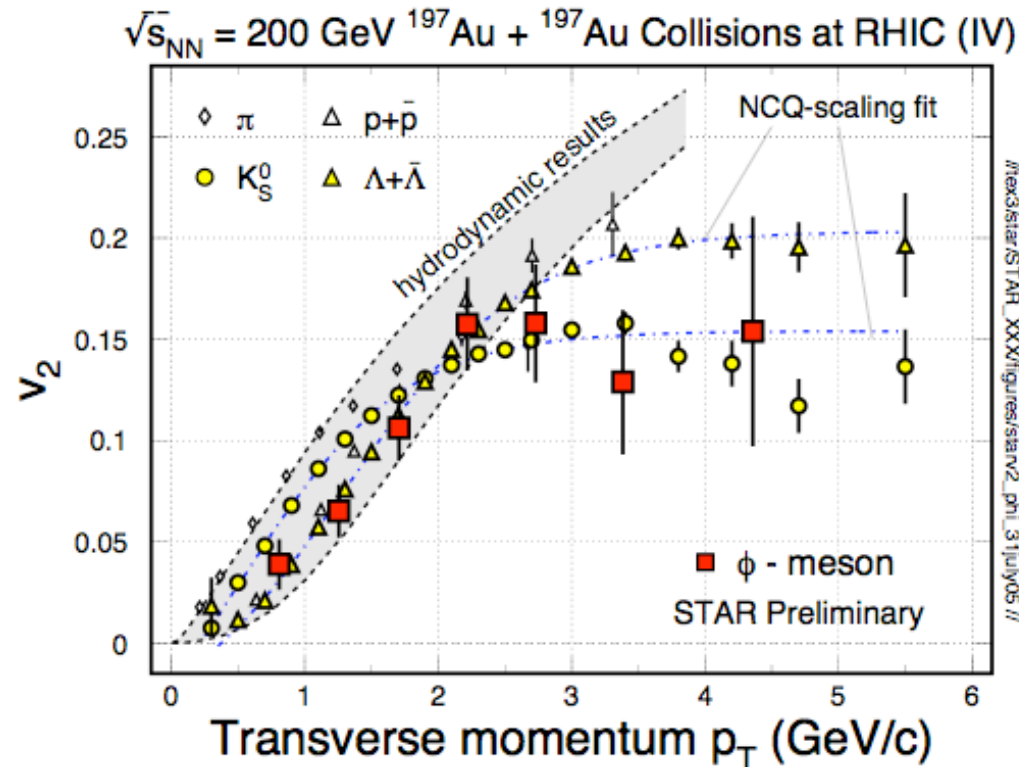


# $v_2$ at Low $p_T$ Region



- Minimum bias data!
- At low  $p_T$ , model result fits mass hierarchy well - Collective motion at RHIC
- More work needed to fix the details in the model calculations.

# $\phi$ -mesons Flow: Partonic Flow

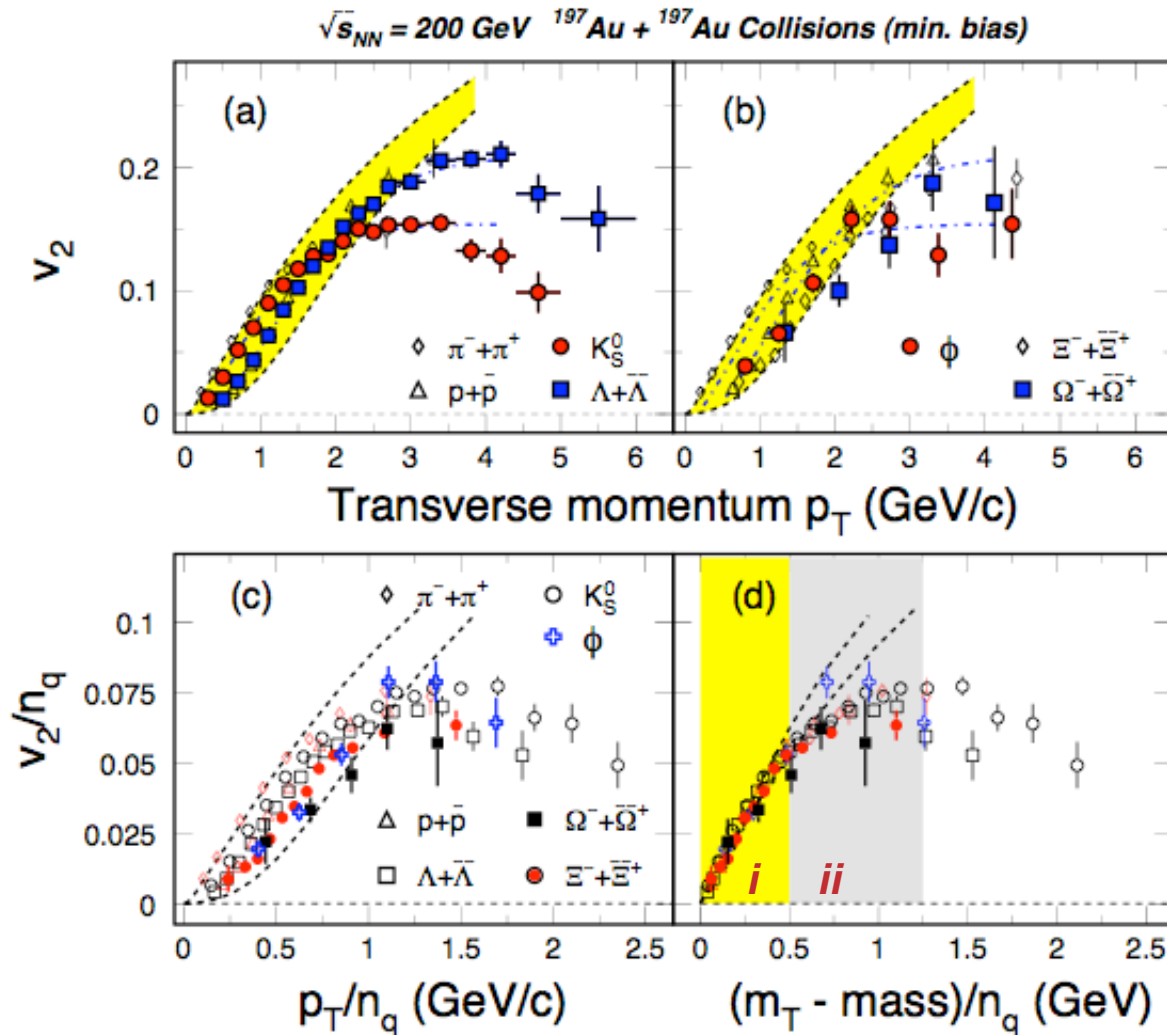


**$\phi$ -mesons are very special:**

- they do not re-interact in hadronic environment
- they show strong collective flow
- they are formed via coalescence with thermal s-quarks

STAR Preliminary: SQM06, S. Blyth

Hwa and Yang, *nucl-th/0602024*; Chen et al., *PRC73* (2006) 044903



- $v_2$  of light hadrons and multi-strange hadrons
- scaling by the number of quarks

At RHIC:

⇒  $m_T$  - NQ scaling

⇒ De-confinement

PHENIX: PRL91, 182301(03)

STAR: PRL92, 052302(04), 95, 122301(05)  
nucl-ex/0405022, QM05

S. Voloshin, NPA715, 379(03)

Models: Greco et al, PRC68, 034904(03)

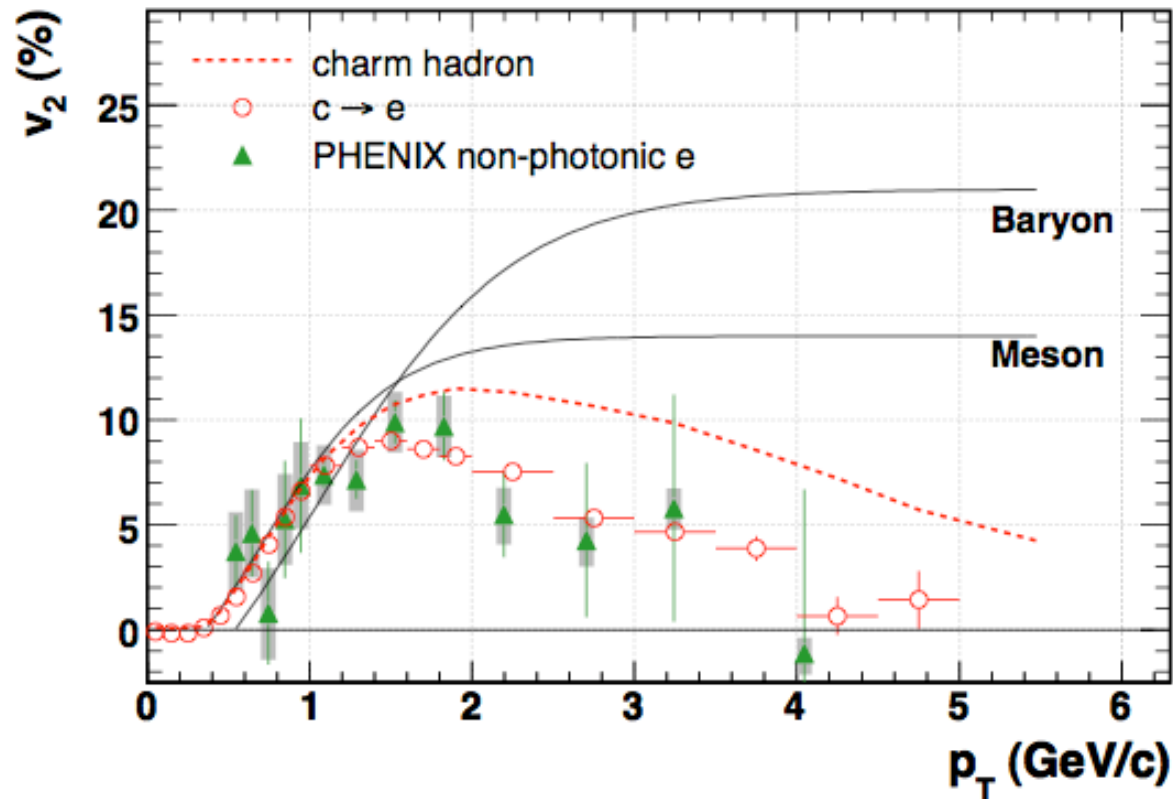
Chen, Ko, nucl-th/0602025

Nonaka et al. PLB583, 73(04)

X. Dong, et al., Phys. Lett. B597, 328(04).

....

# Non-photonic Electron $v_2$



PHENIX: Minimum bias

Yifei Zhang

M. Kaneta *et al*, J.Phys. **G30**, S1217(04)

STAR Ph.D student

HSD: E. Bratkovskaya *et al.*, hep-ph/0409071; X. Dong, S. Esumi, *et al.*, Phys. Lett. **B597**, 328(2004).

## In central Au+Au collisions at RHIC

### - partonic freeze-out:

$$*T_{\text{pfo}} = 165 \pm 10 \text{ MeV}$$

weak centrality dependence

$$v_{\text{pfo}} \geq 0.2 (c)$$

### - hadronic freeze-out:

$$*T_{\text{fo}} = 100 \pm 5 \text{ (MeV)}$$

strong centrality dependence

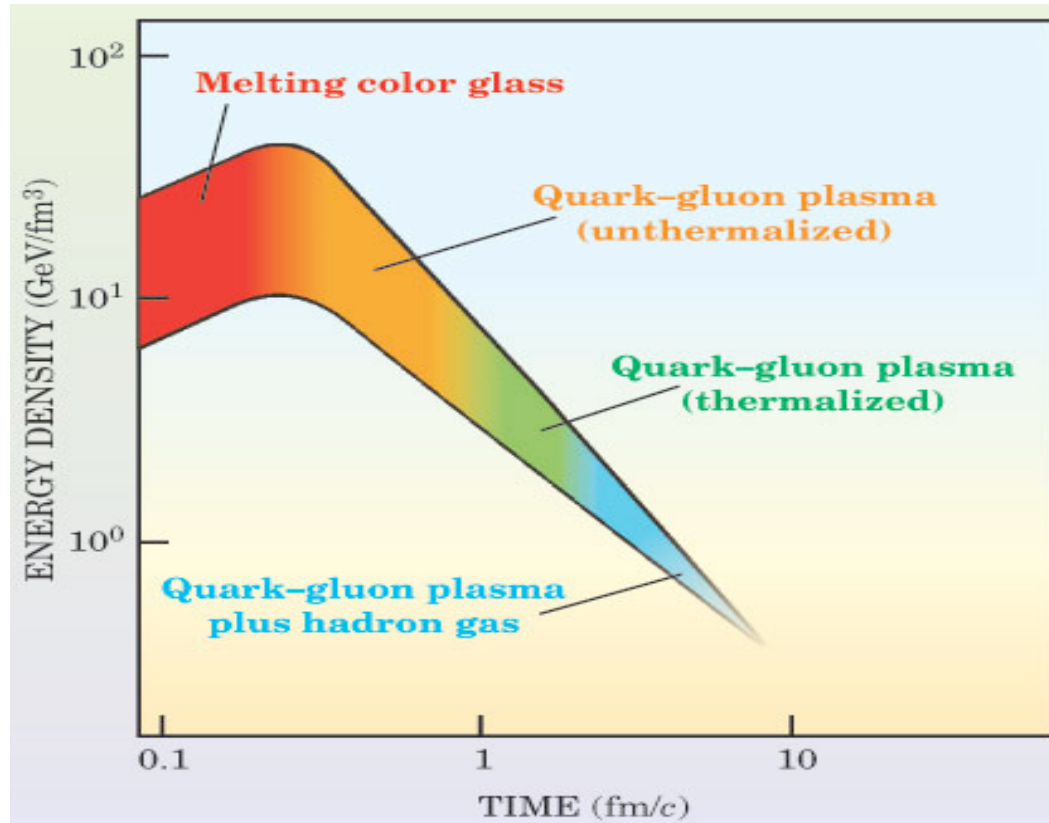
$$v_{\text{fo}} = 0.6 \pm 0.05 (c)$$

Systematic study are needed to understand the centrality dependence of the EoS parameters

*\* Thermalization assumed*

## Physics Today

L. McLerran, T. Ludlam,



### Jet-quenching:

Hot and dense system created in Au+Au collisions

### Flow:

Collective flow observed for all hadrons especially the multi-strange and charm hadrons. The partonic interactions are responsible to the early collectivity at RHIC

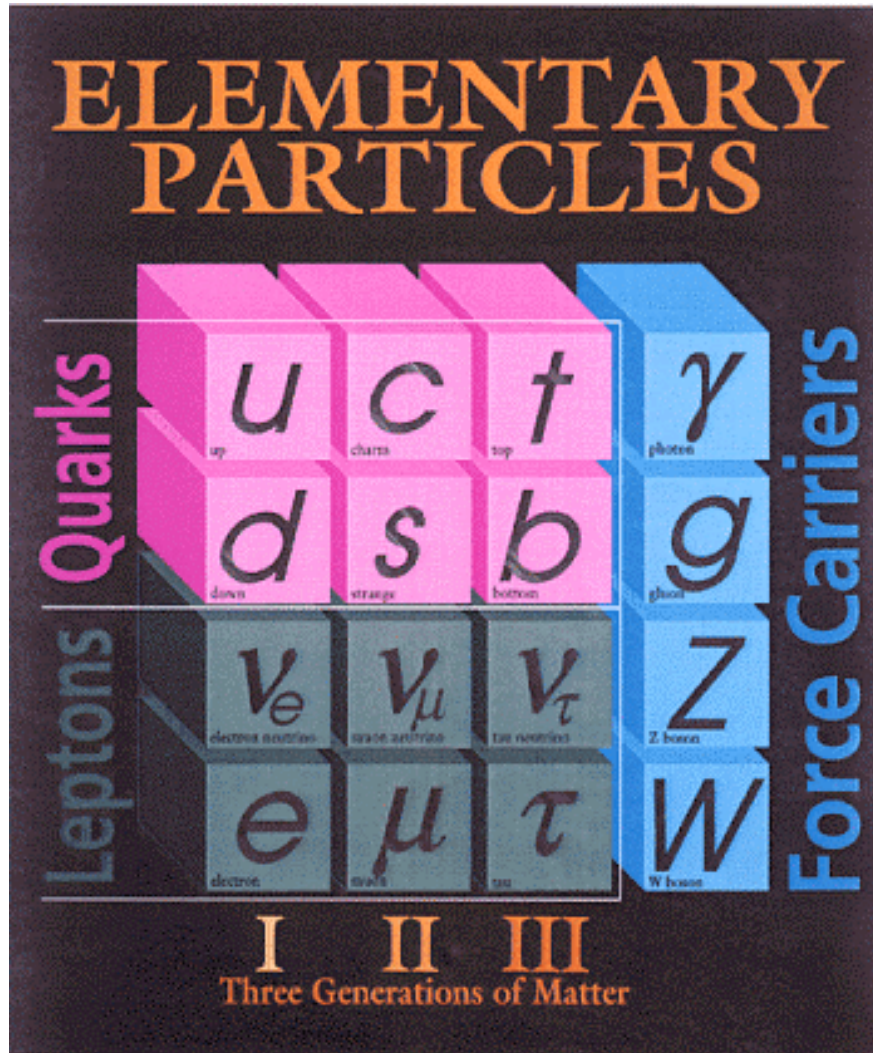
### Next Step:

**Test thermalization of light flavors by studying heavy flavor collectivity**

# In the Near Future



# Quantum Chromodynamics

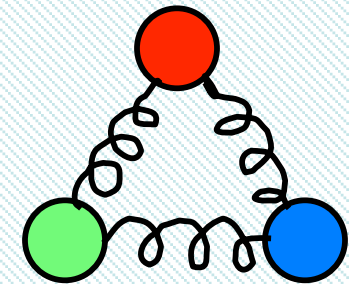


- 1) Quantum Chromodynamics (QCD) is the established theory of strongly interacting matter.
- 2) Gluons hold quarks together to form hadrons:

meson

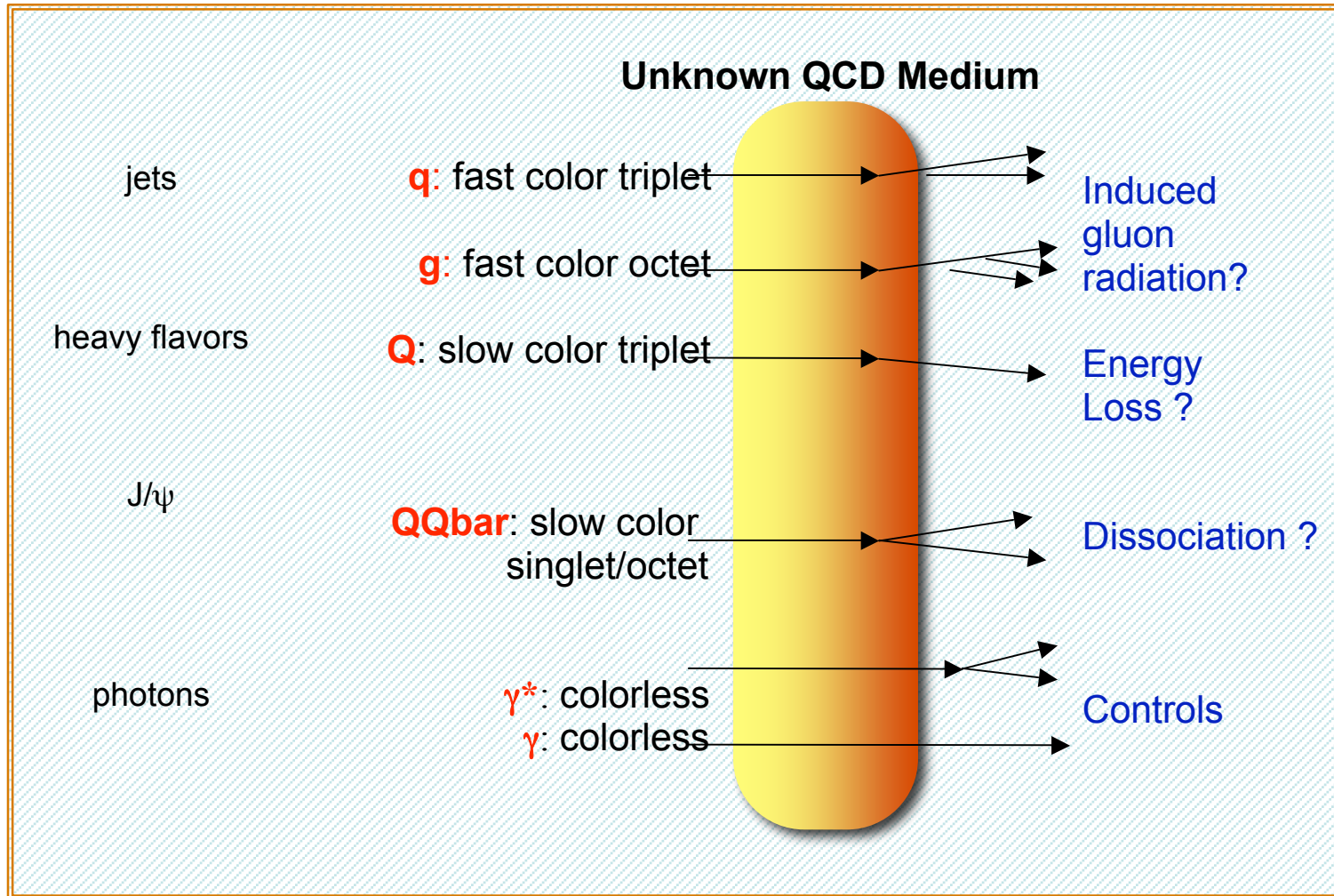


baryon



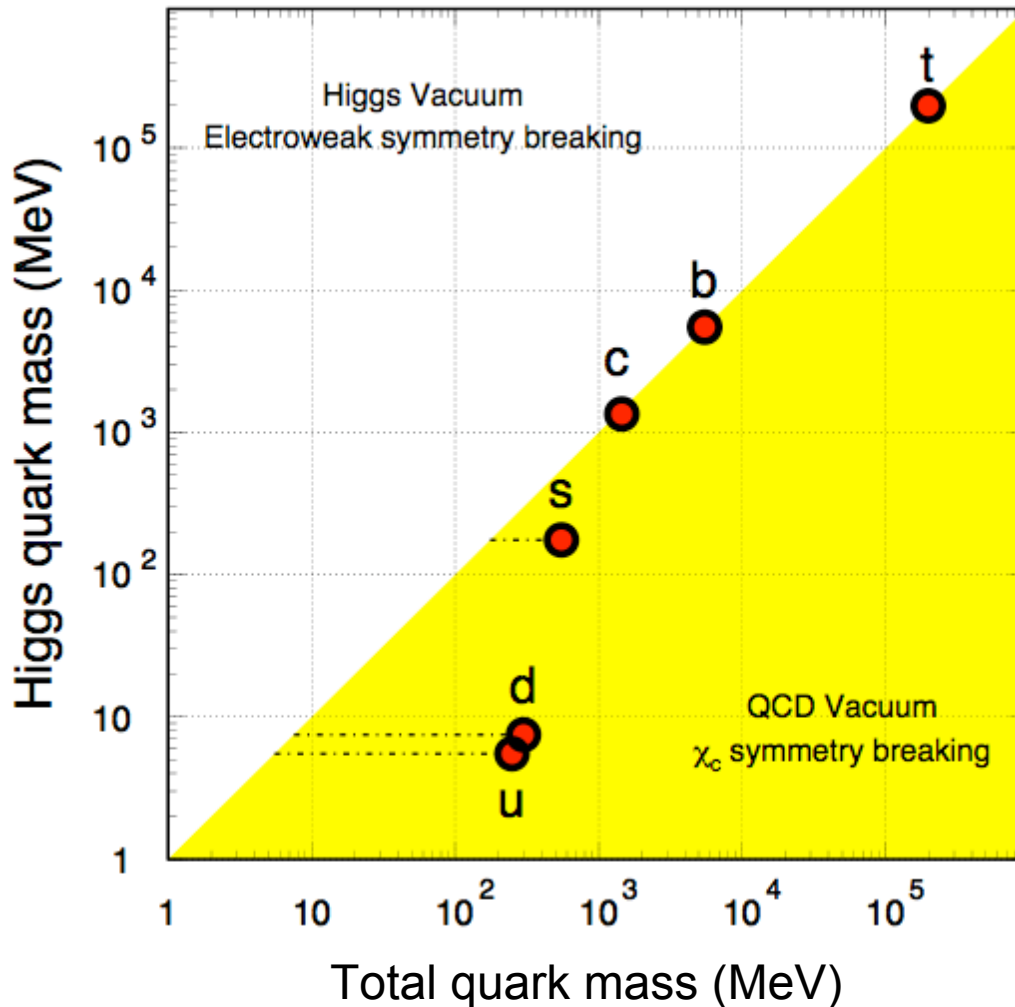
- 3) Gluons and quarks, or partons, typically exist in a color singlet state: confinement.





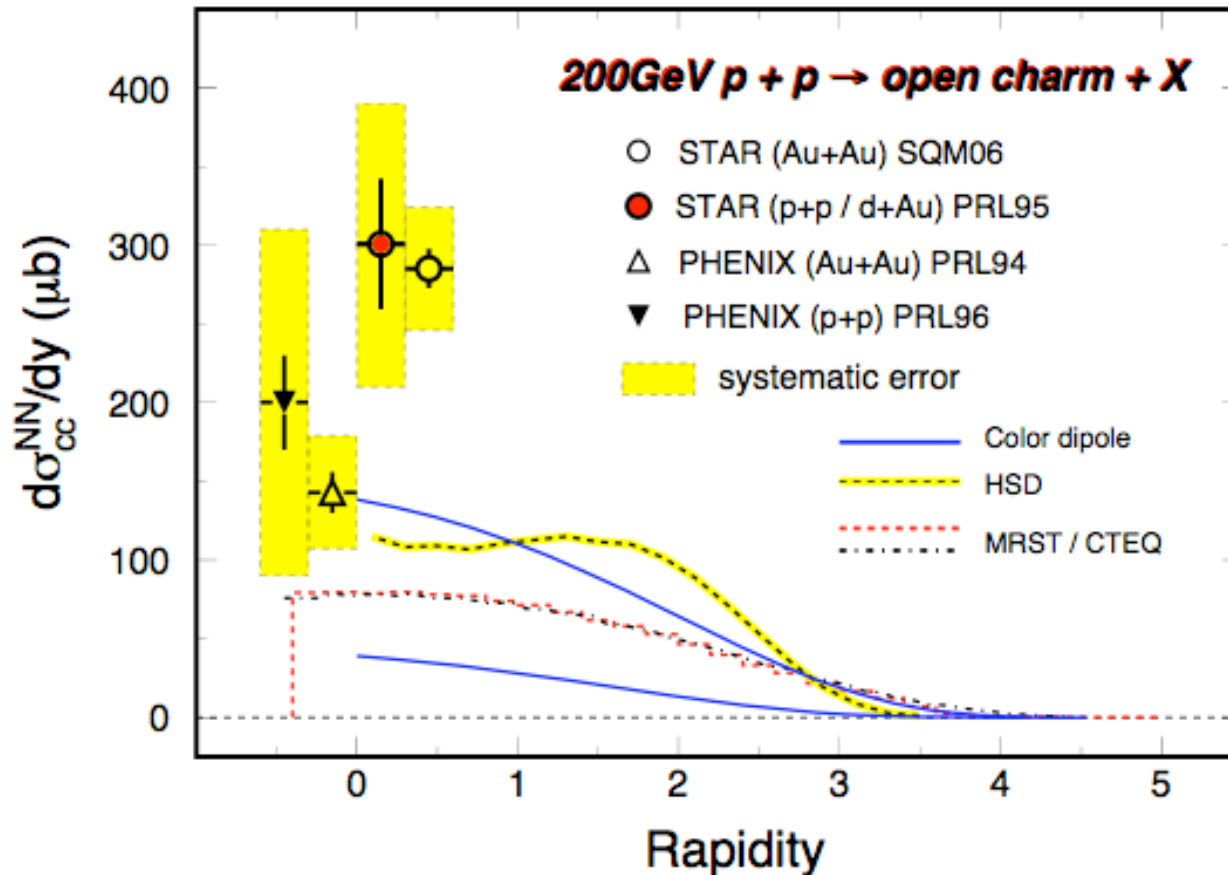
$$d\sigma_{AB \rightarrow \text{hard}}(b) = T_{AB}(b) \cdot d\sigma_{pp \rightarrow \text{hard}} \quad T_{AB}(b) \propto N_{bin}(b)$$

# Quark Masses



- 1) Higgs mass: electro-weak symmetry breaking. (current quark mass)
  - 2) QCD mass: Chiral symmetry breaking. (constituent quark mass)
- ⇒ Strong interactions do not affect heavy-quark masses.
- ⇒ Important tool for studying properties of the hot/dense medium at RHIC.
- ⇒ Test pQCD predictions at RHIC.

# Charm Cross Section Results



mid-y data

STAR:

$e^\pm, \mu^\pm, D, e-K$

PHENIX:

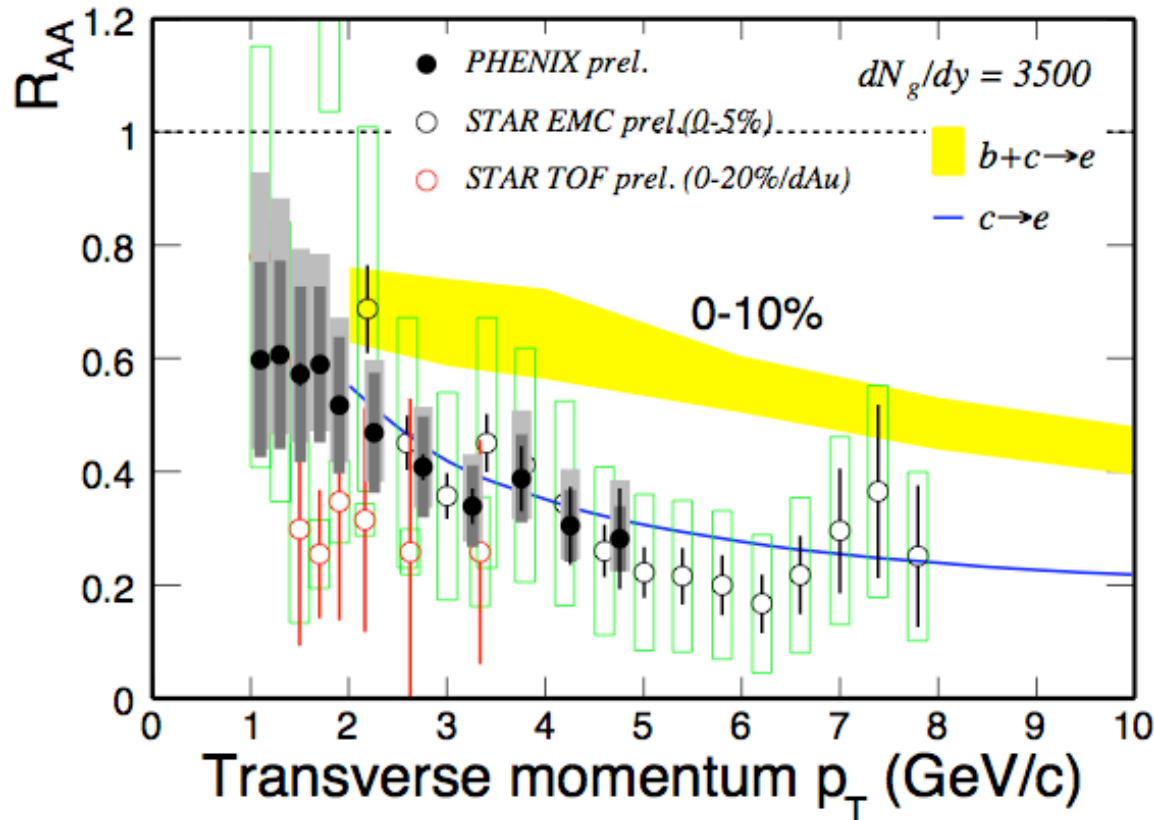
$e^\pm$

First set of measurements:

- 1) Number of binary collision scaling  $\Rightarrow$  initial production
- 2) pQCD models under-predict charm cross sections
- 3) Systematic errors are large. Precision data are needed.

# Heavy Flavor Energy Loss

M. Djordjevic, et. al. [nucl-th/0507019](#)



1) Non-photonic electrons decayed from  $b$ -charm and beauty hadrons

2) At  $p_T \geq 6$  GeV/c,

$$R_{AA}(n.e.) \sim R_{AA}(h^\pm)$$

contradicts to naïve pQCD predictions

## Surprising results -

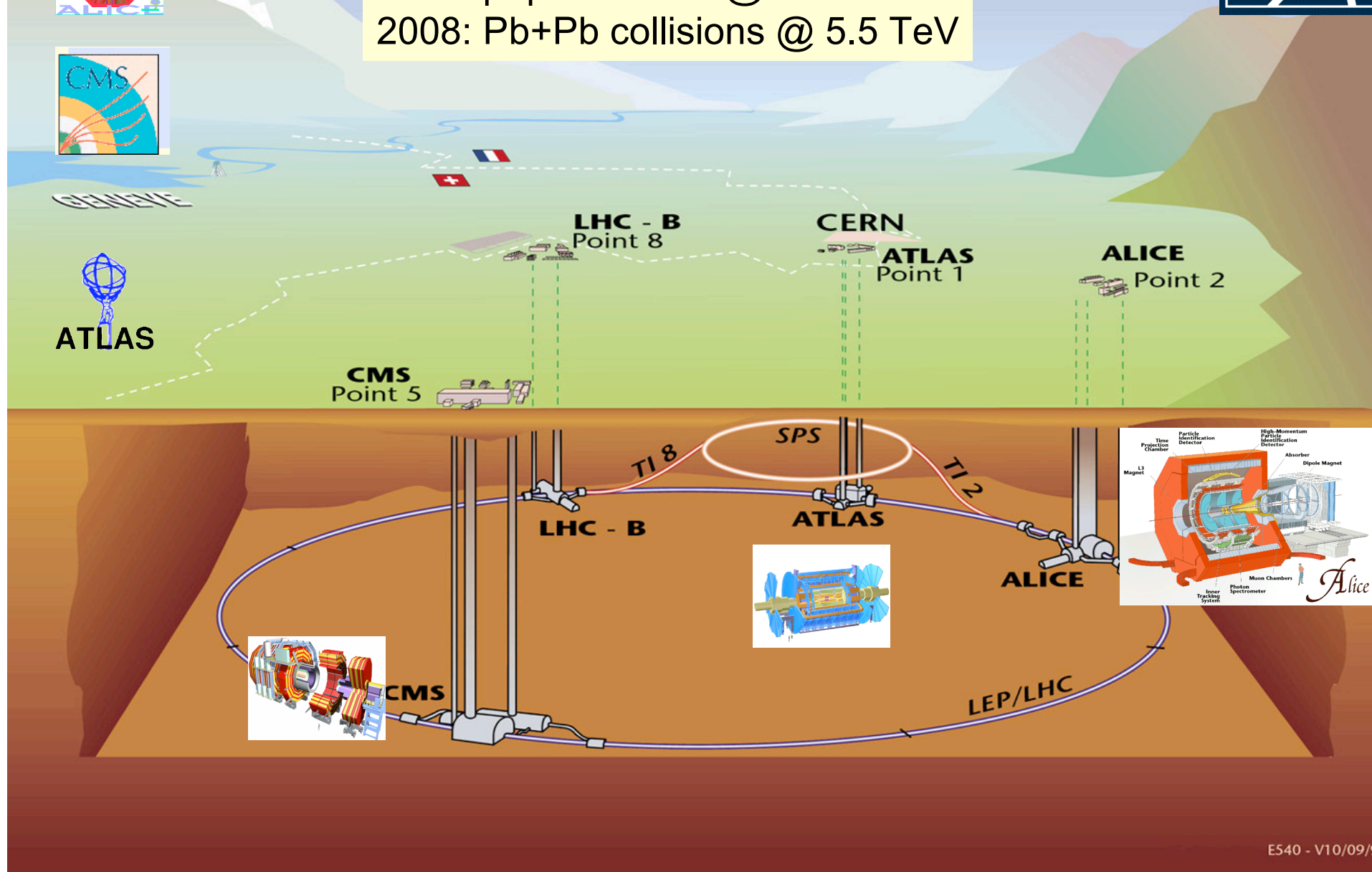
- challenge our understanding of the energy loss mechanism
- force us to RE-think about the collision energy loss
- requires isolation of c-hadrons contributions from b-hadrons



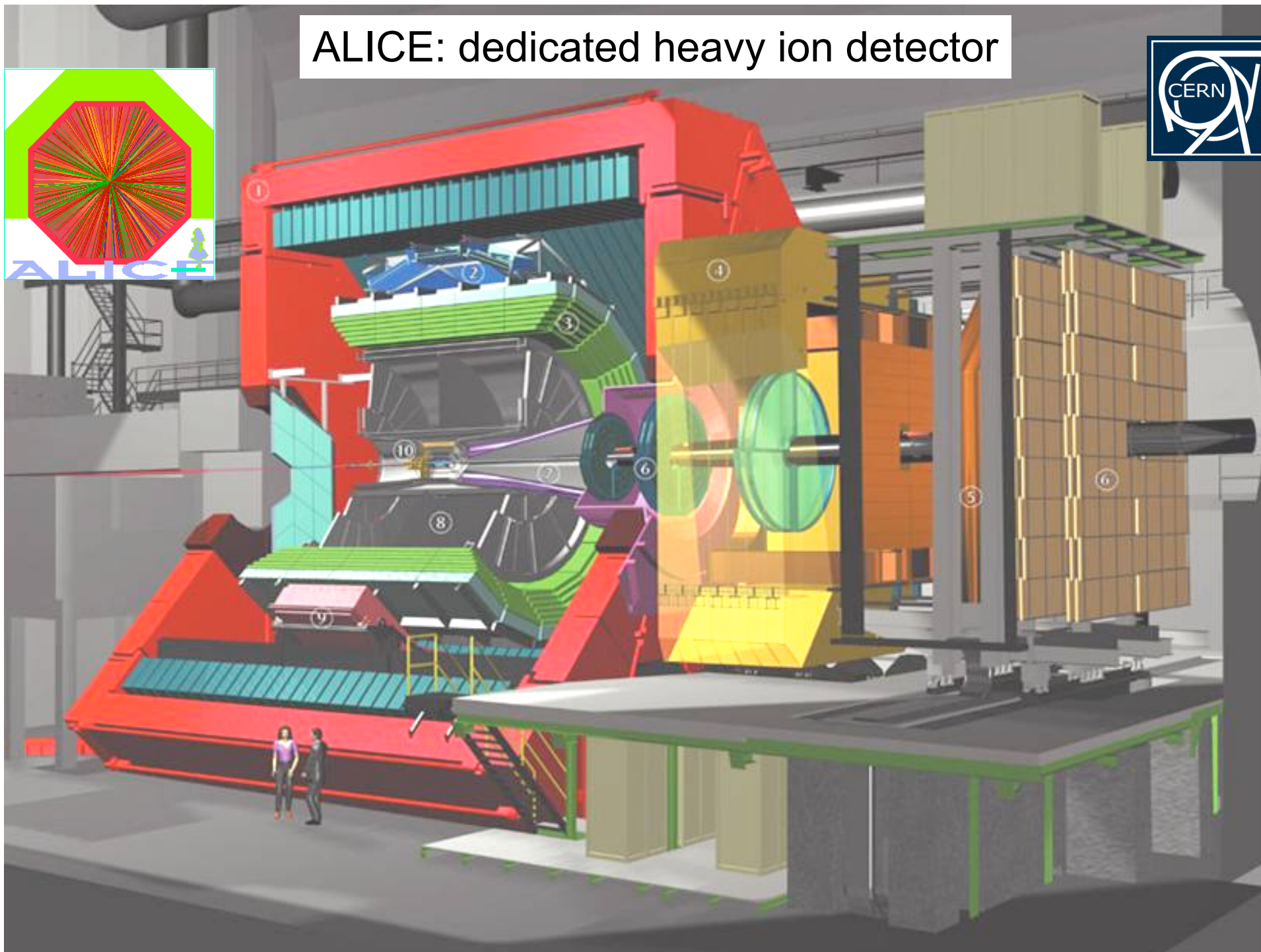
# Overall view of the LHC experiments.



2007: p+p collisions @ 14 TeV  
2008: Pb+Pb collisions @ 5.5 TeV



# ALICE: dedicated heavy ion detector



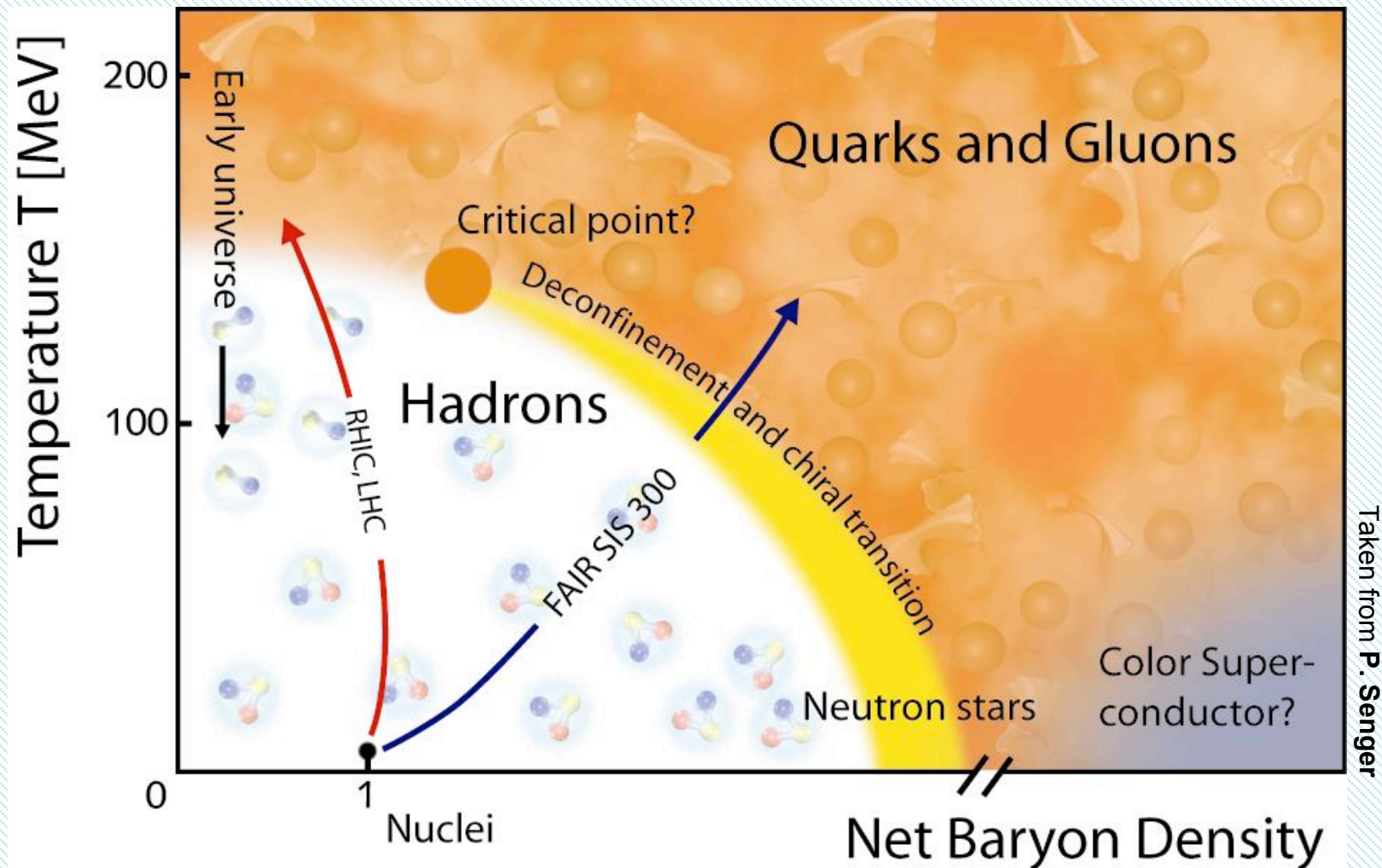
## RHIC upgrades and new LHC programs:

(now-2012)

(2008)

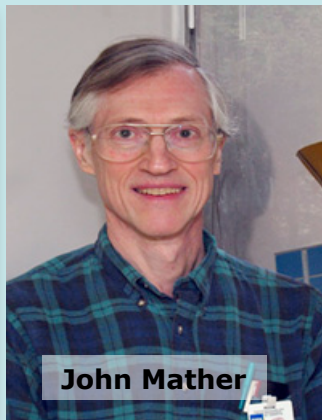
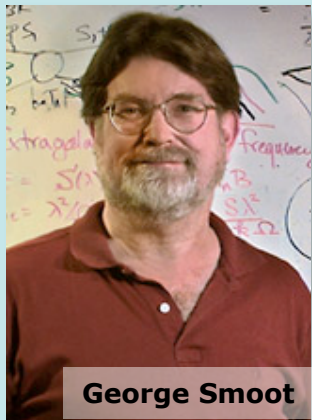
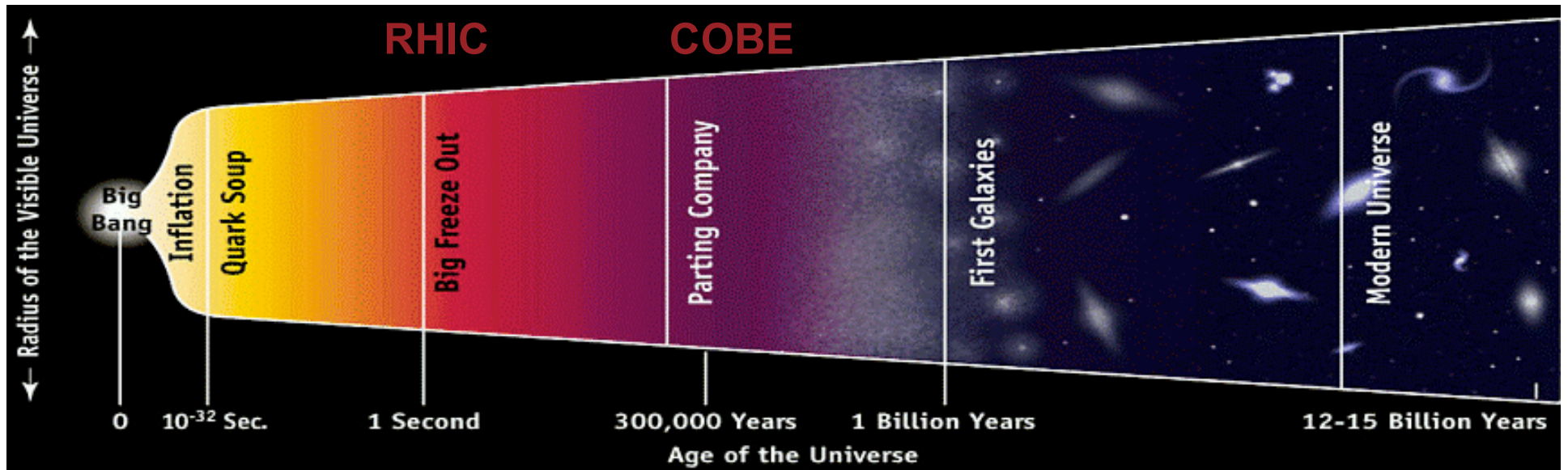
- high  $p_T$  c-hadron spectra
  - ⇒ pQCD properties in hot/dense medium
- precise data on total cross section for c- and b-hadrons
- c-hadron correlation functions and flow
  - ⇒ heavy flavor collectivity and light flavor **thermalization**
- more surprises: ...
  - ⇒ **New era for understanding the QCD medium properties at both RHIC and LHC is coming.**





- 1) RHIC heavy-flavor program / LHC:
  - Study **medium properties**
  - pQCD in hot and dense medium
- 2) RHIC energy scan / GSI program:
  - Search for **phase boundary**.
  - Chiral symmetry restoration

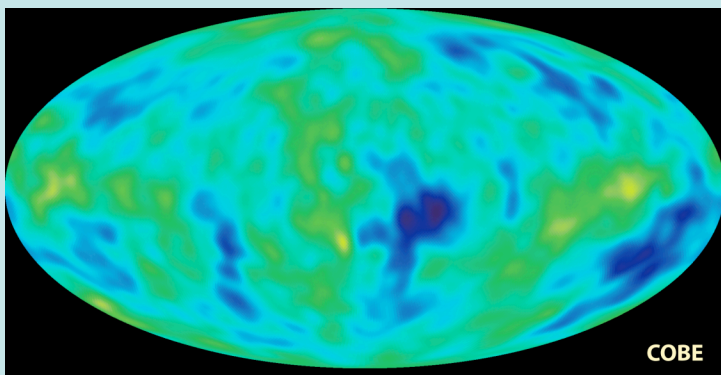




## The Nobel Prize in Physics 2006

<http://www.lbl.gov/Publications/Nobel/>

"for their discovery of the blackbody form and anisotropy of the cosmic microwave background radiation"



**COBE:** Discovery 'baby photo' of the universe

**RHIC:** Life history of the universe